

# Eads, Eiffel and the Forth Bridge

The big 19<sup>th</sup> century  
iron and **steel** bridges

1. How arches carry load: Eads Bridge
2. Two hinged arches: Garabit
3. Details of form in metal arches: Garabit and Mungstener
4. Influence of structural failure on subsequent design
5. Strength and safety in cantilever form: Forth Bridge

# But first!

- An exercise to help with next week's homework and to help us identify the skills of your friends and neighbors in the class.
- Let's do a little statics exercise in the style of a *magazine quiz*, give yourself a point each time you know the answer to the questions that follow – we will sum points to find our statics gurus!

# Q1

- In two dimensions what are the three equations of equilibrium?
  - (1)
  - (2)
  - (3)
  
- Give yourself a point if you know them.

# Answer 1

- In two dimensions what are the three equations of equilibrium?
  - (1)  $\Sigma F_x = 0$
  - (2)  $\Sigma F_y = 0$
  - (3)  $\Sigma M = 0$
- Give yourself a point if you know them.

## Q2

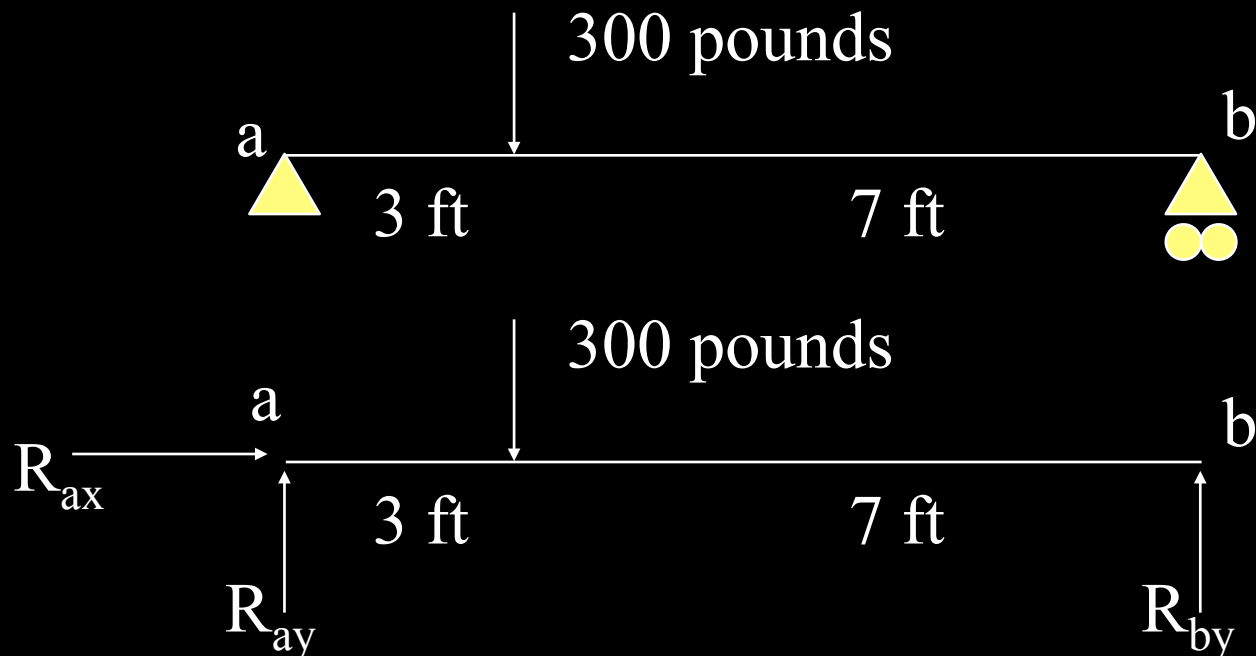
- Make a free body diagram of the following little bridge.



- Give yourself a point if you know how. 😊

# Answer 2

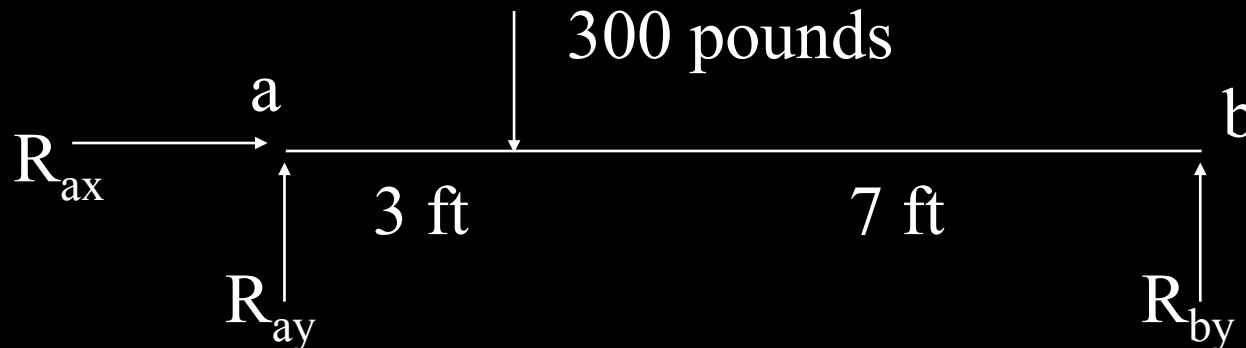
- Make a free body diagram of the following little bridge.



- Give yourself a point if you know how. 😊

# Q3

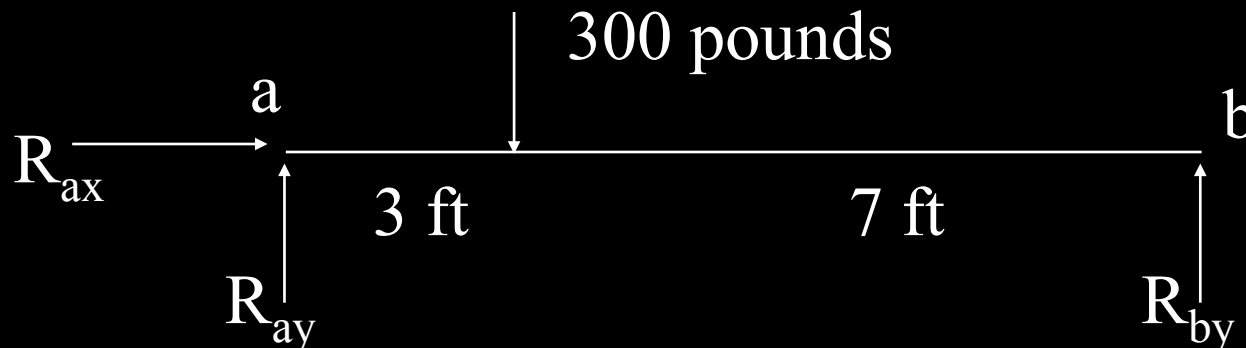
- Write the equation for sum of forces in the y



- Give yourself a point if you know how. 😊

# Answer 3

- Write the equation for sum of forces in the y



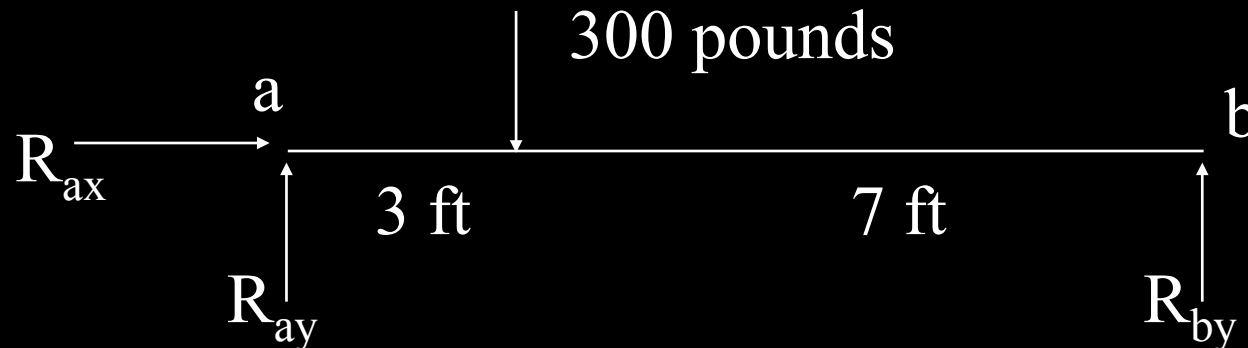
$$\Sigma F_y = 0 \quad R_{ay} - 300 + R_{by} = 0 \quad R_{ay} + R_{by} = 300$$

- Give yourself a point if you know how. 😊



# Q4

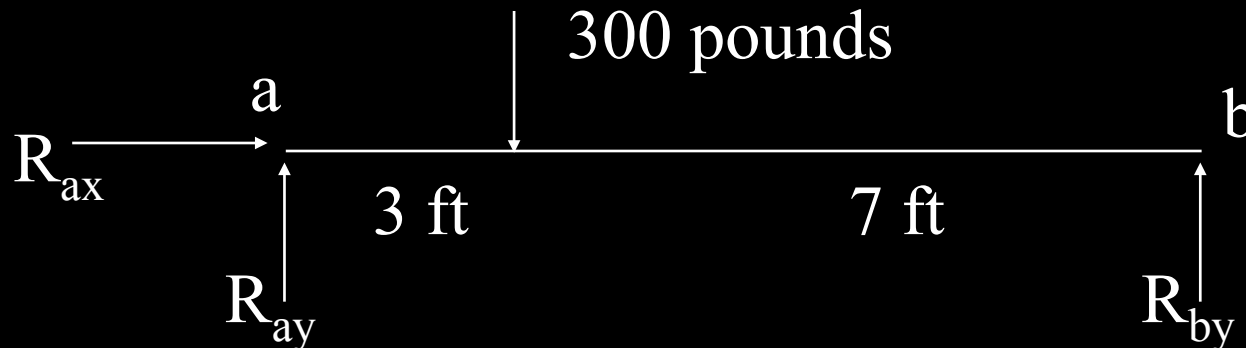
- Write the equation for sum of moments at a



- Give yourself a point if you know how. 😊

# Answer 4

- Write the equation for sum of moments at a



$$\Sigma M_a = 0 \quad 10\text{ft} * R_{by} - 3\text{ft} * 300\text{lbs} = 0$$

$$R_{by} = 90\text{lbs}$$

$$\& R_{ay} = 300 - 90 = 210\text{lbs}$$

- Give yourself a point if you know how. 😊

# Q5

- I enjoy helping others because it helps me to understand concepts better too.
- Give yourself a point if you agree with the above statement.

# Totals

- 1 – No worries, but expect to ask some questions of your new friends and neighbors (and just wait until I ask them to draw or write.. 😊)
- 2 – Hey this stuff is new to me! That's OK, lean on your friend and neighbors a bit
- 3 – Statics is neither your friend nor your enemy - help and be helped!
- 4 – Great, you know a lot and can help others, please do so!
- 5 – Statics Guru with a positive attitude. Your help is needed and expected!

# Moving time (just for today)

- Establish the 3's, 4's and 5's..
- Find our way into groups of 2 or 3 – these are not permanent groups, don't fret!
- Introduce yourself

# Moving time (just for today)

- Establish the 3's, 4's and 5's..
- Find our way into groups of 2 or 3 – these are not permanent groups, don't fret!
- Introduce yourself
- Please exchange contact information amongst your group (cell, email, whatever)
- Now we are ready!

# Eads, Eiffel and the Forth Bridge

The big 19<sup>th</sup> century  
iron and **steel** bridges



1850 IRON





1869 IRON





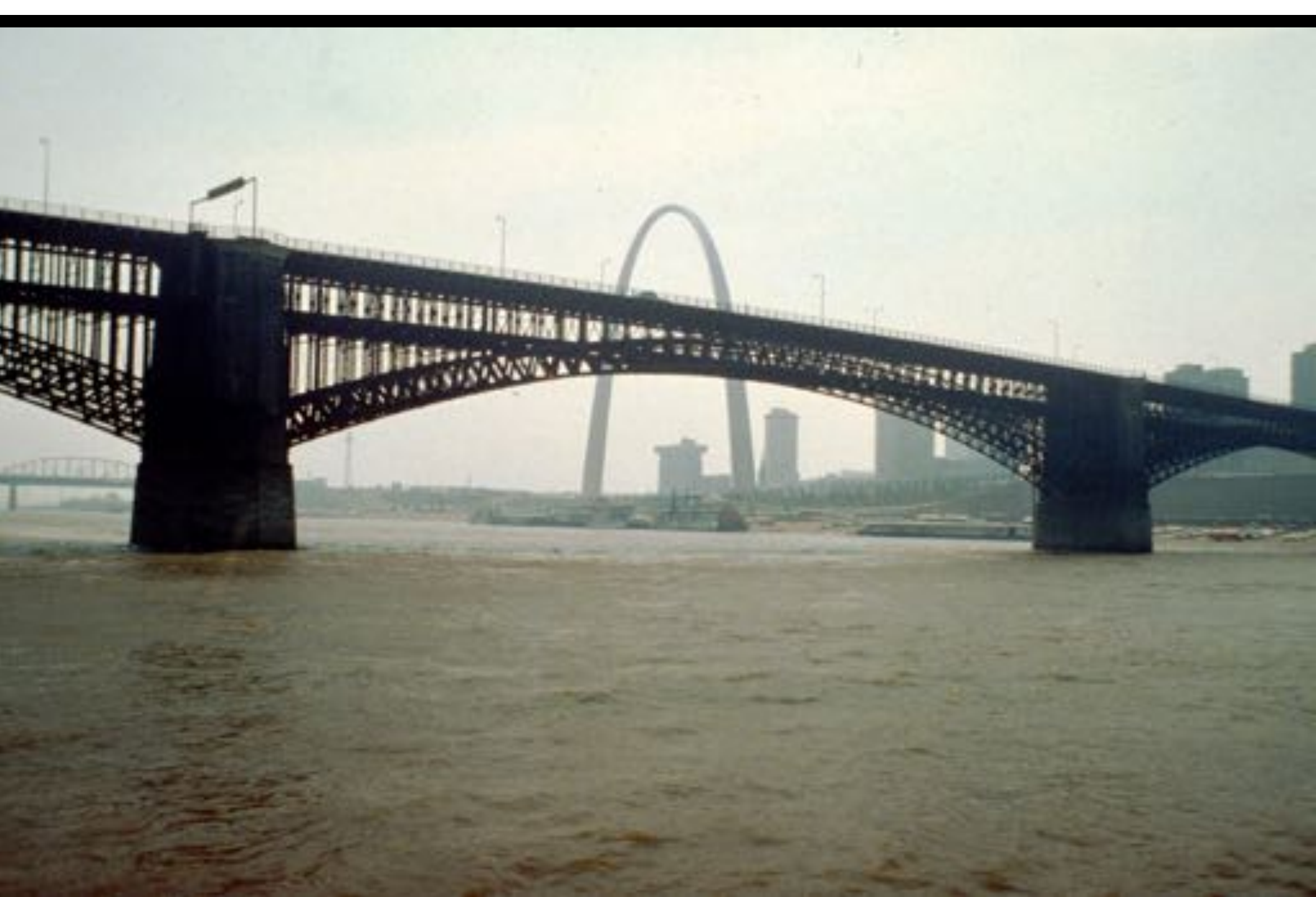
1856 IRON





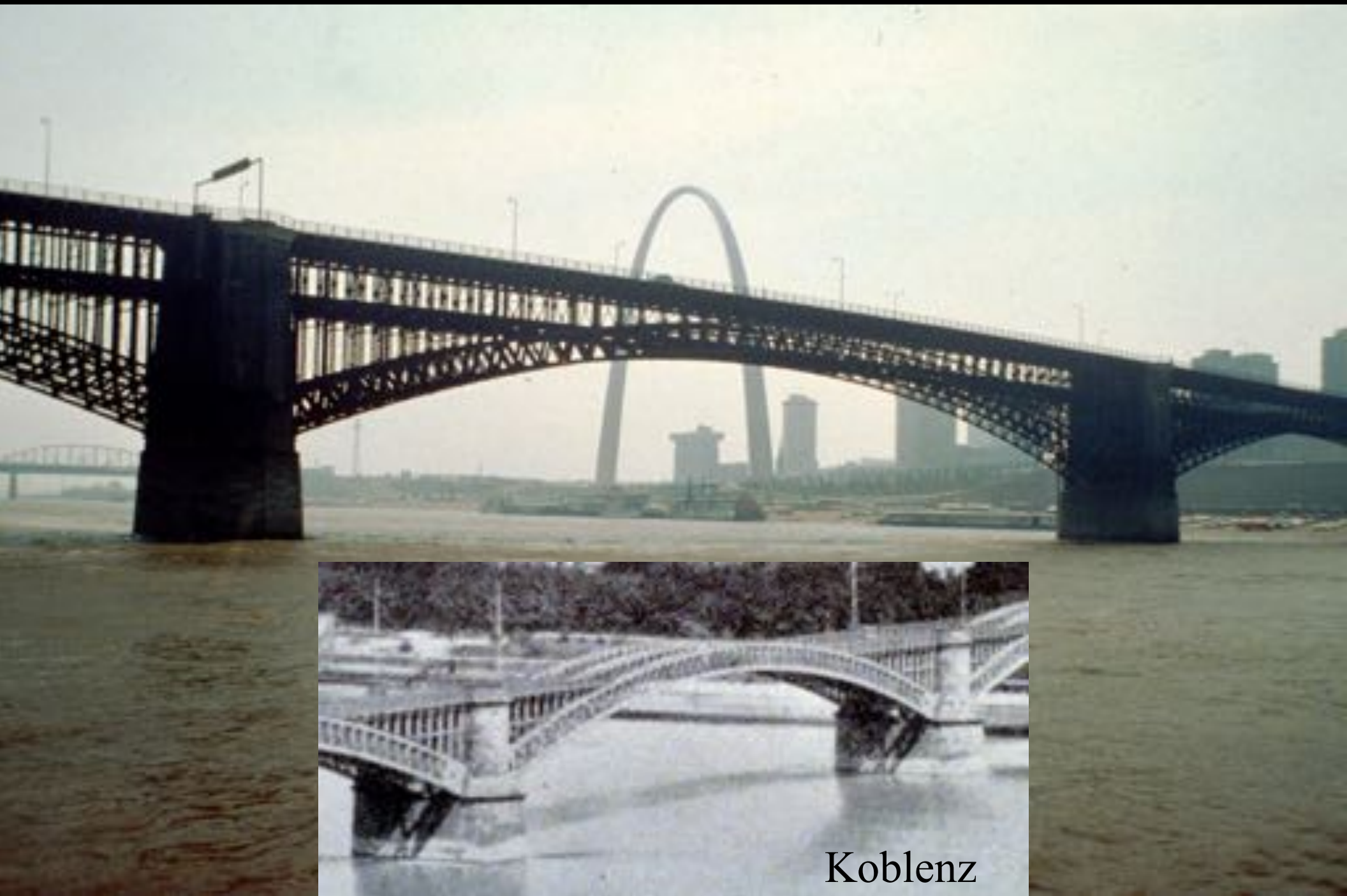


1864 IRON



Eads Bridge - Steel - 520 feet [158 m] - 1874

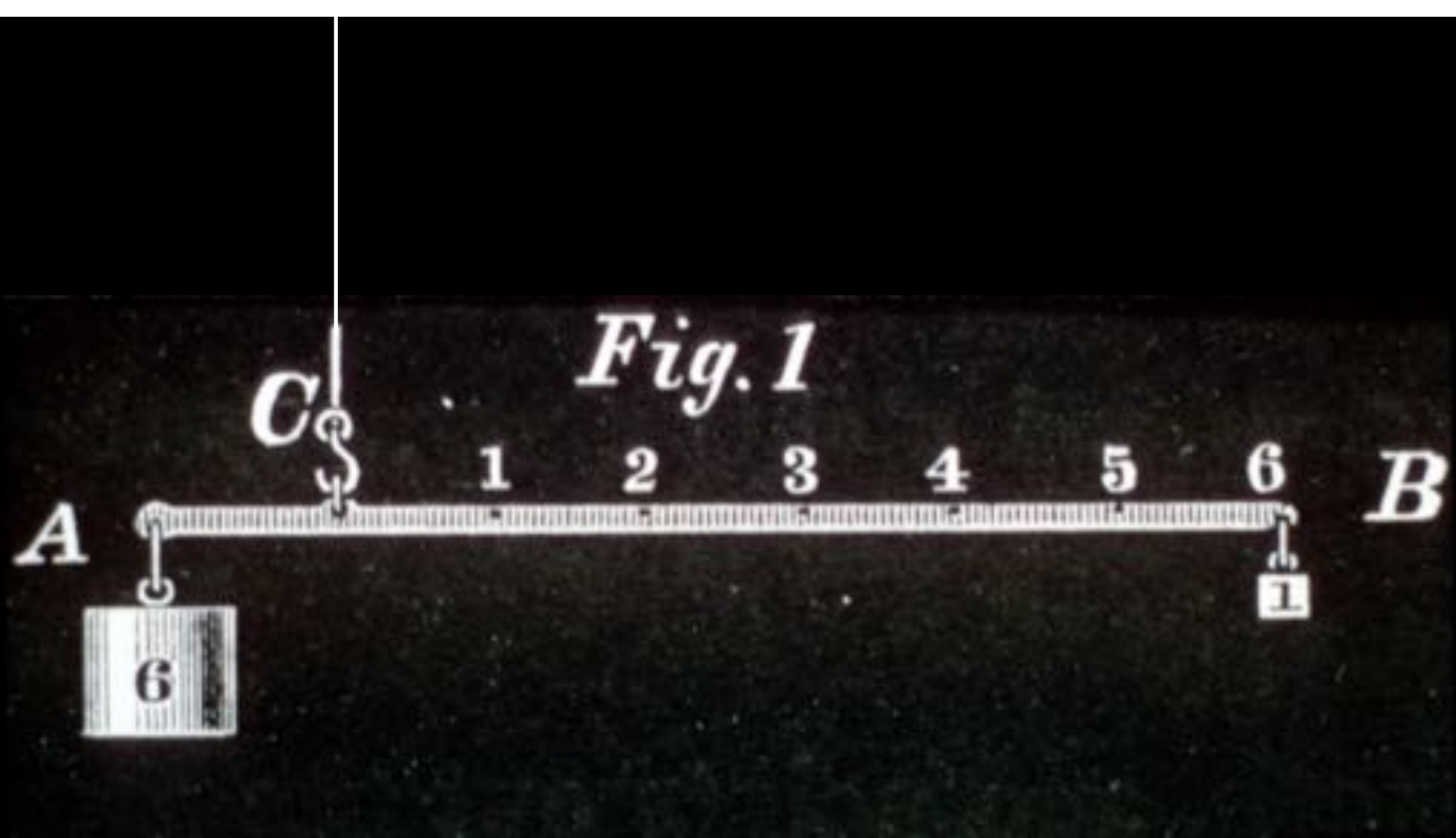




Koblenz



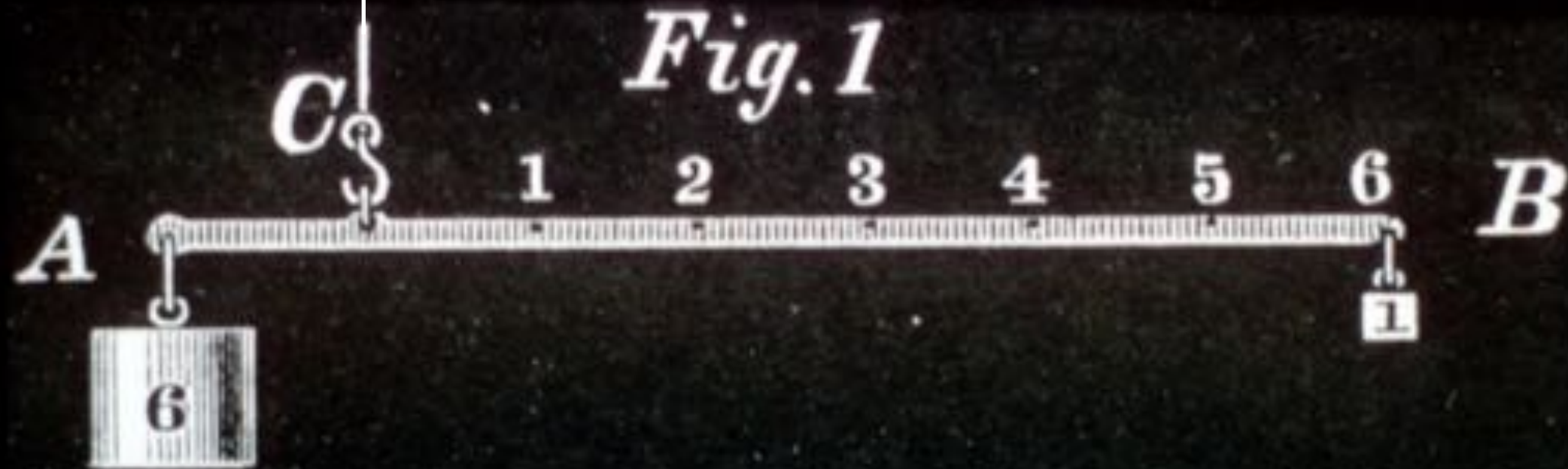
James Buchanan Eads  
1820-1887



From a book written by Eads

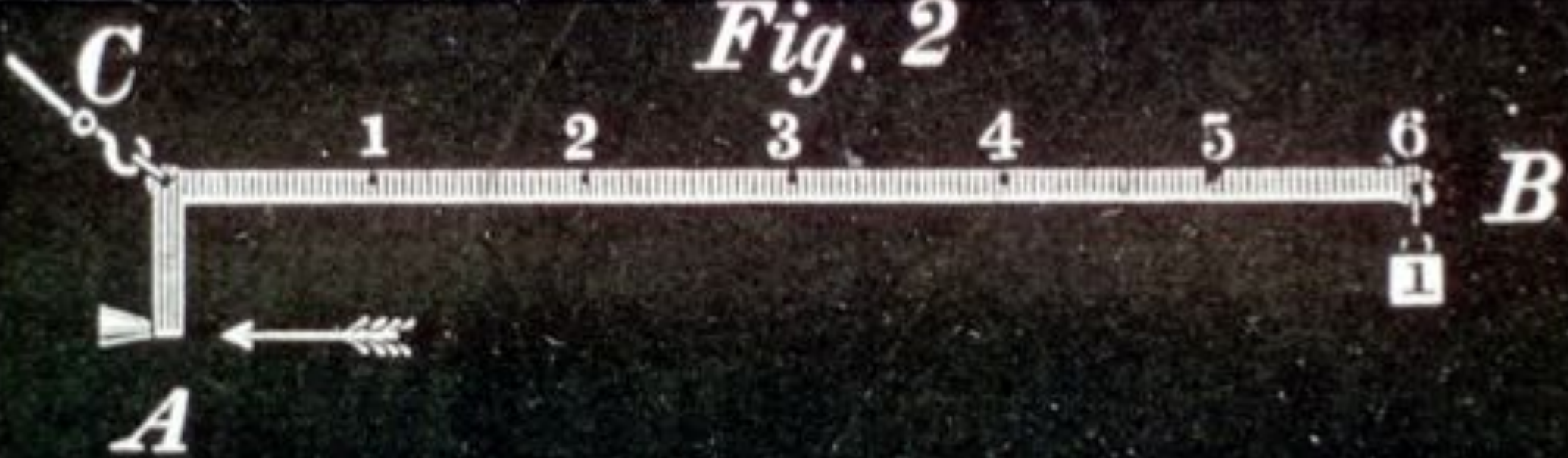


Q: Why doesn't this tip over?

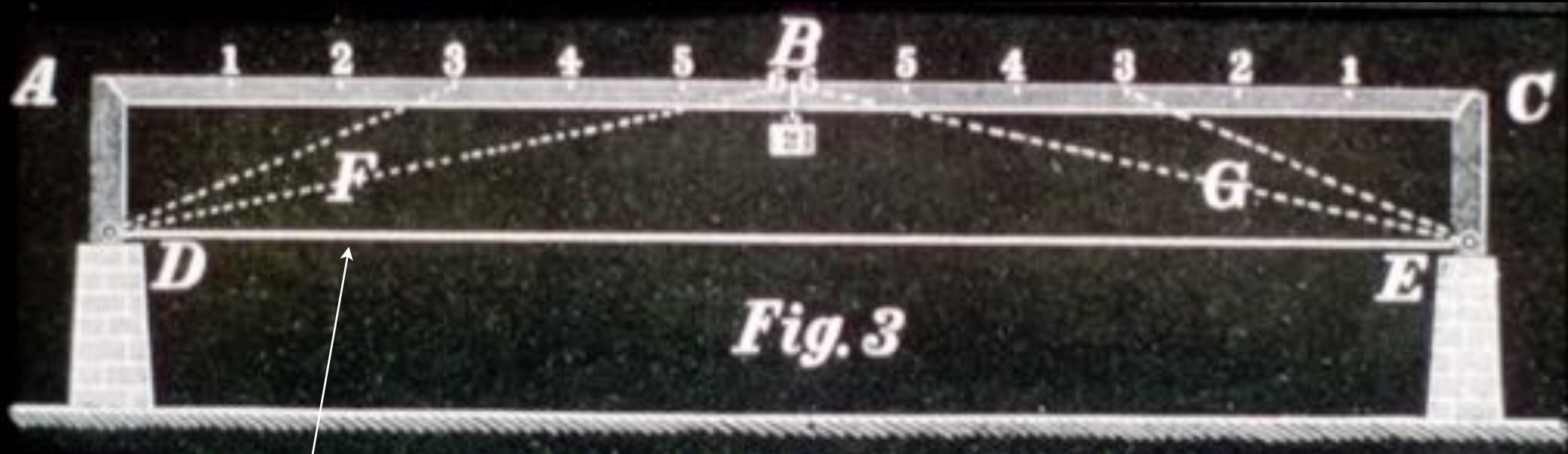




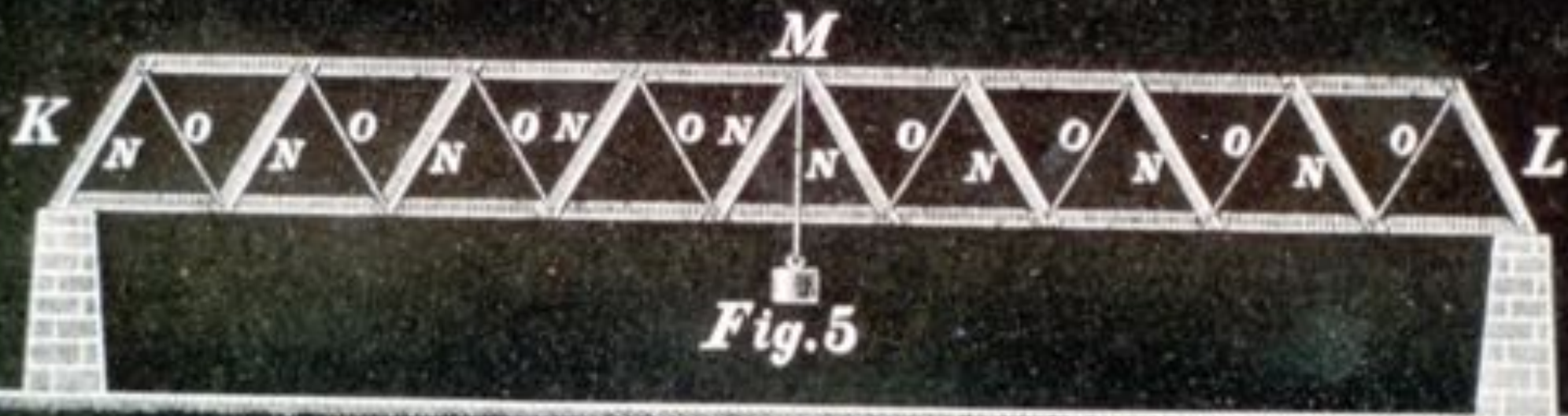
*Fig. 2*



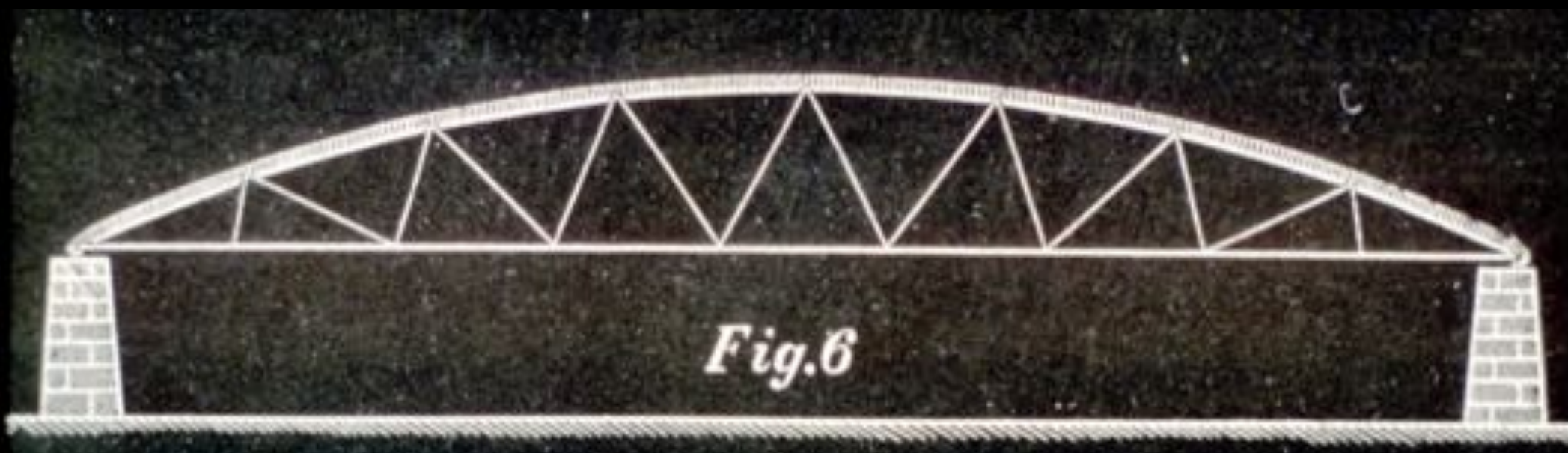
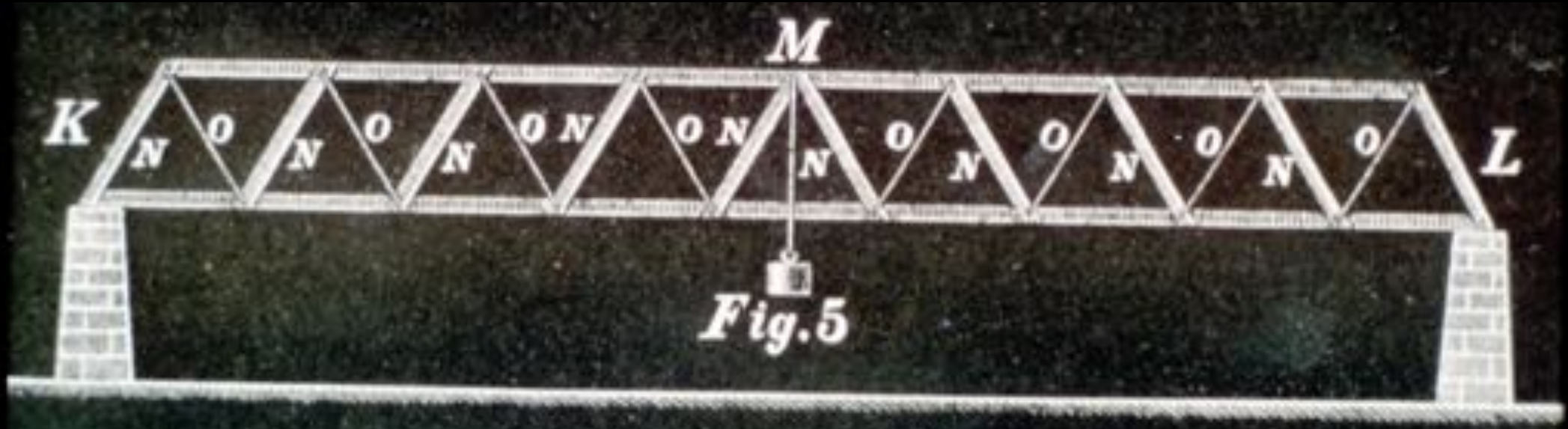




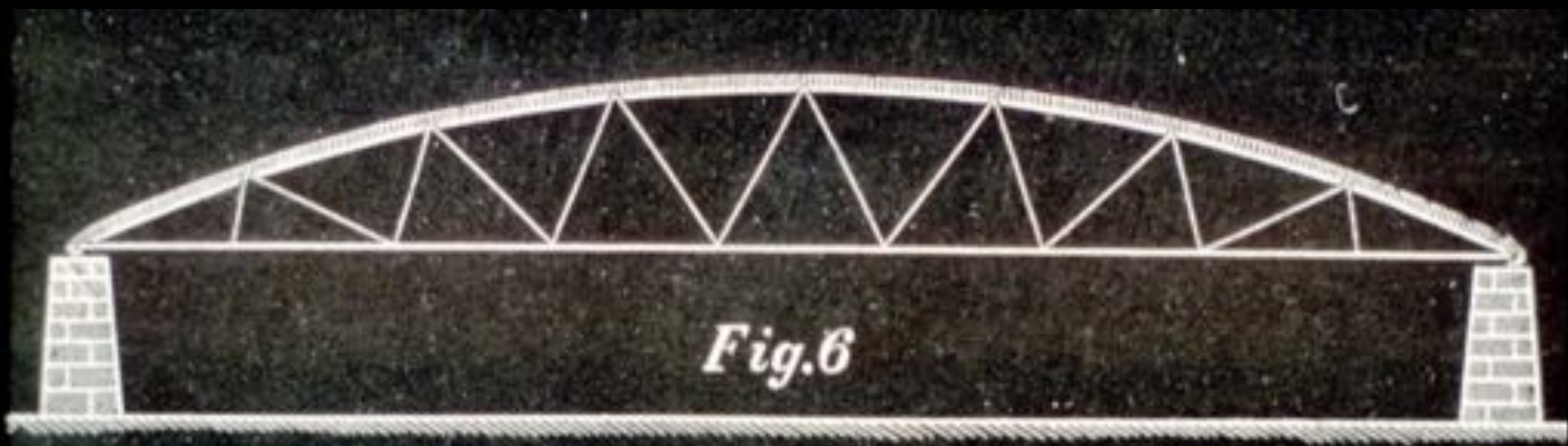
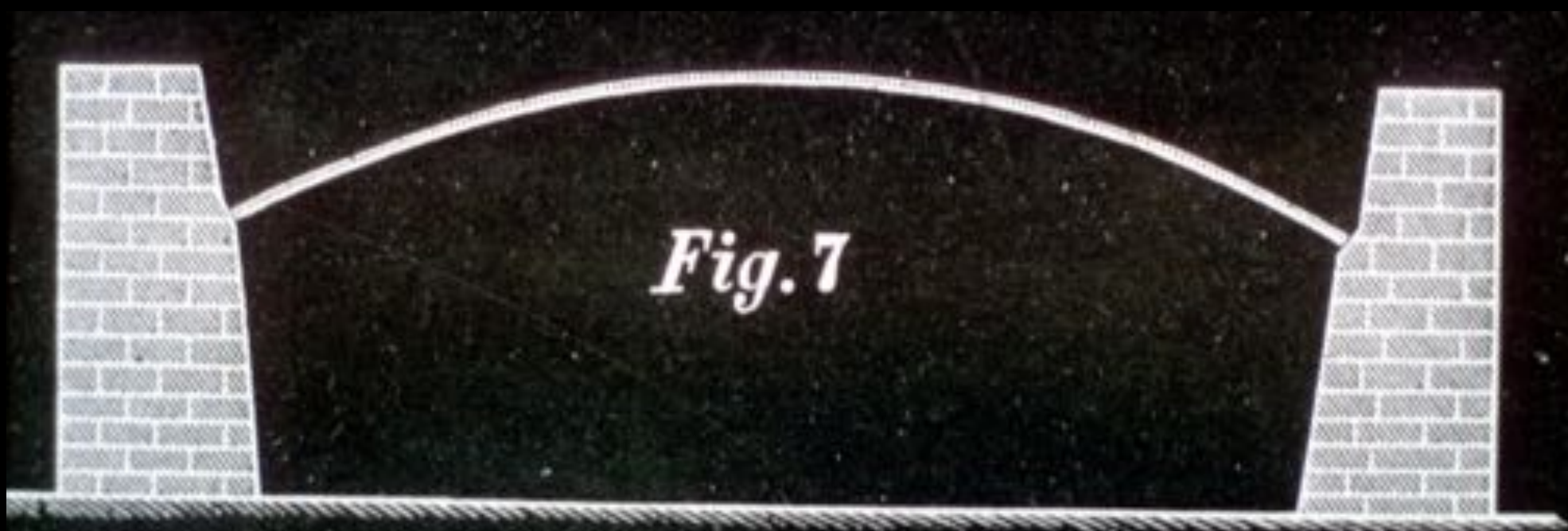
Tension tie provides reaction



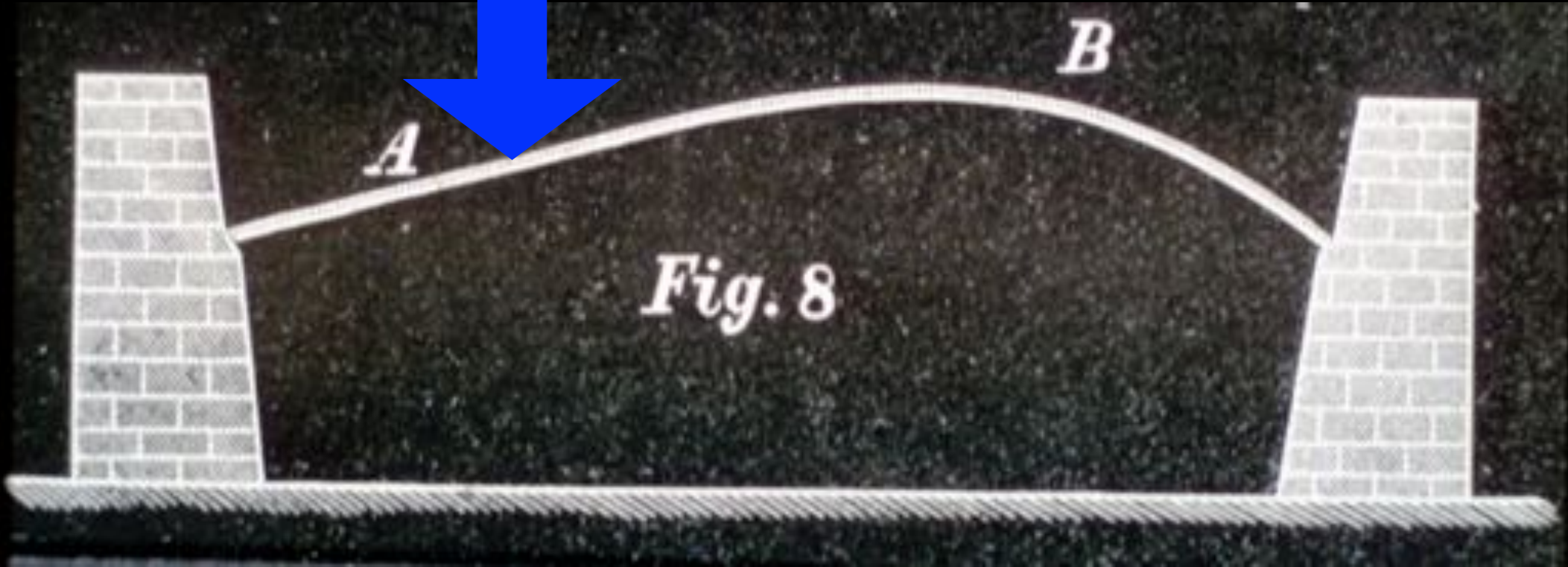
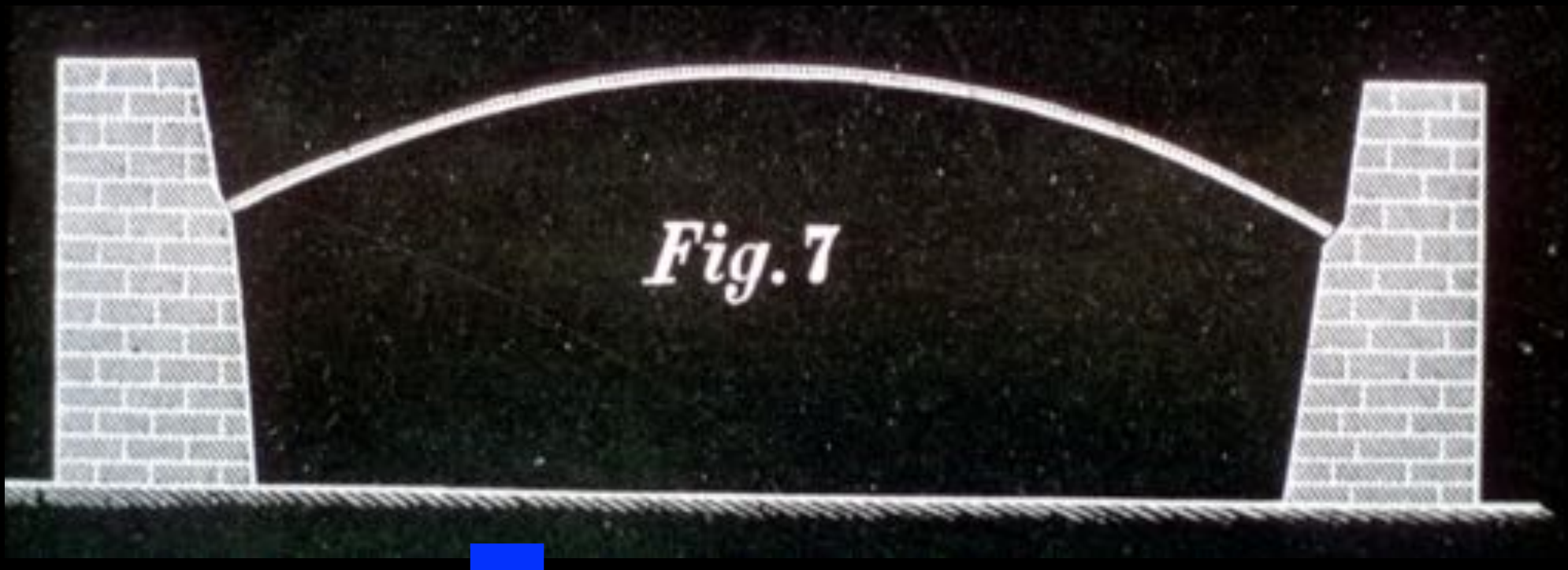




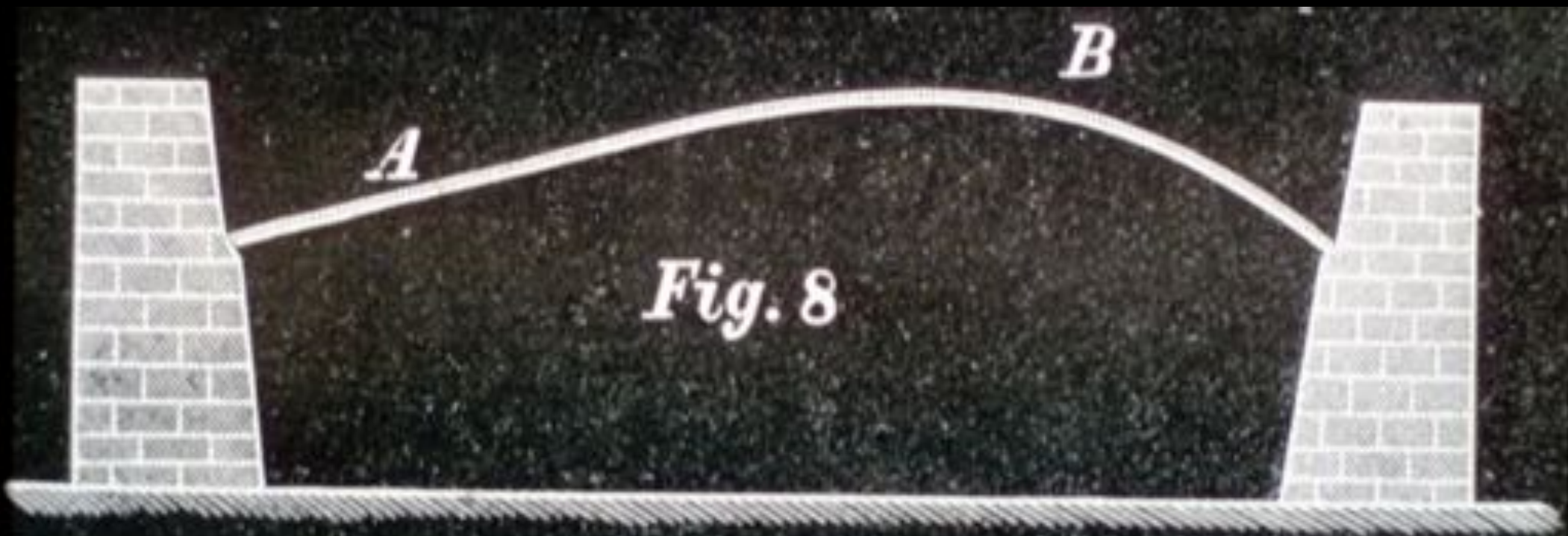








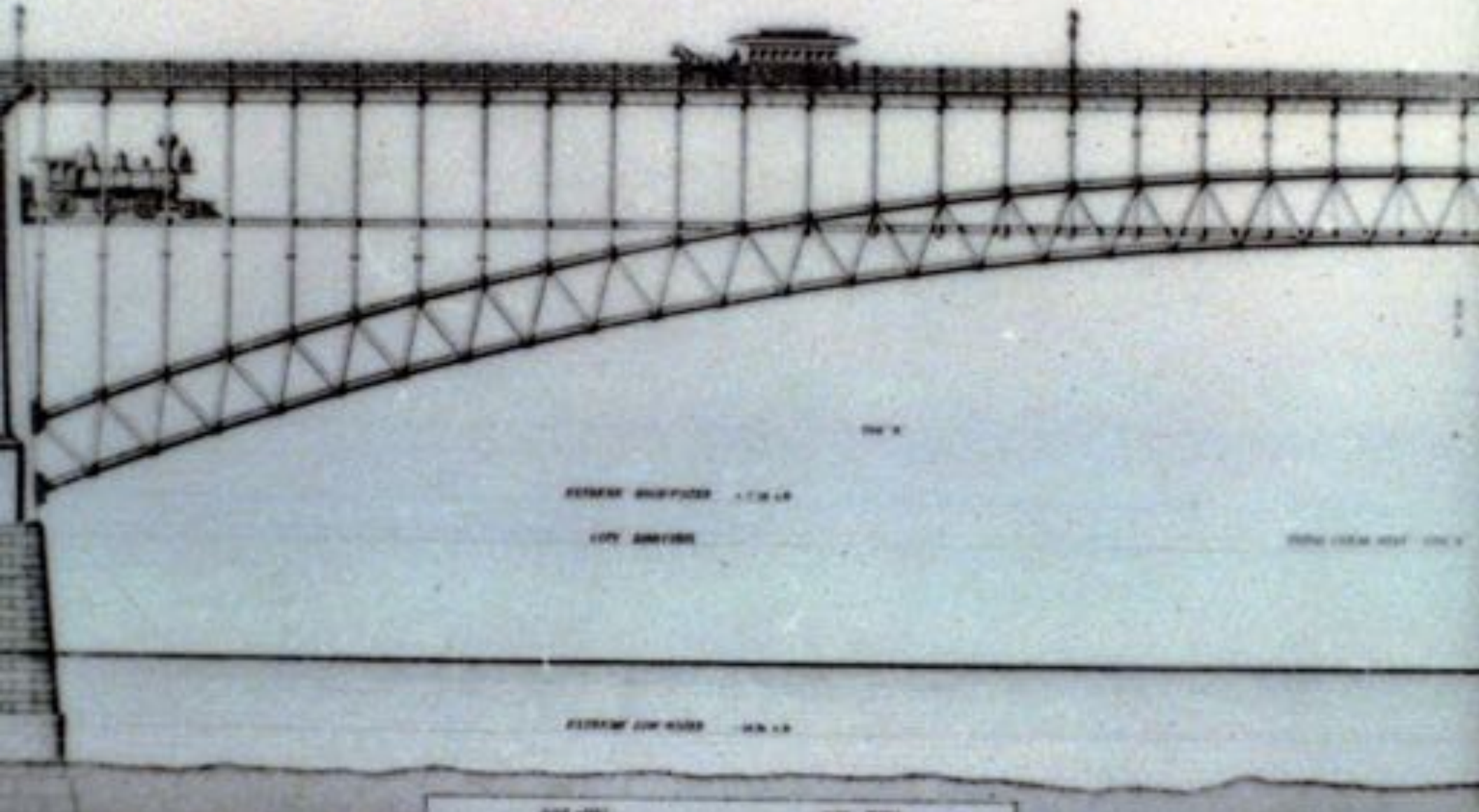








ELEVATION OF ONE-HALF OF  
CENTER SPAN.



EXTREME HIGHER POINT 173.10

LOW POINT

EXTREME LOWER POINT 166.10

EXTREME LOW POINT 166.10

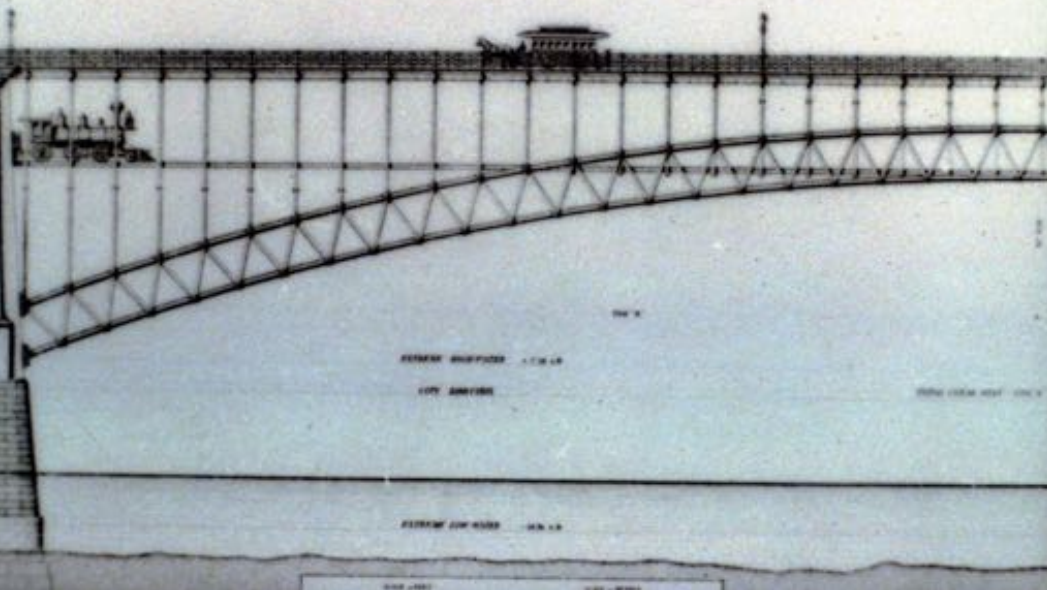
SCALE 1/4" = 10'

SEE PLAN





ELEVATION OF ONE-HALF OF  
CENTER SPAN.

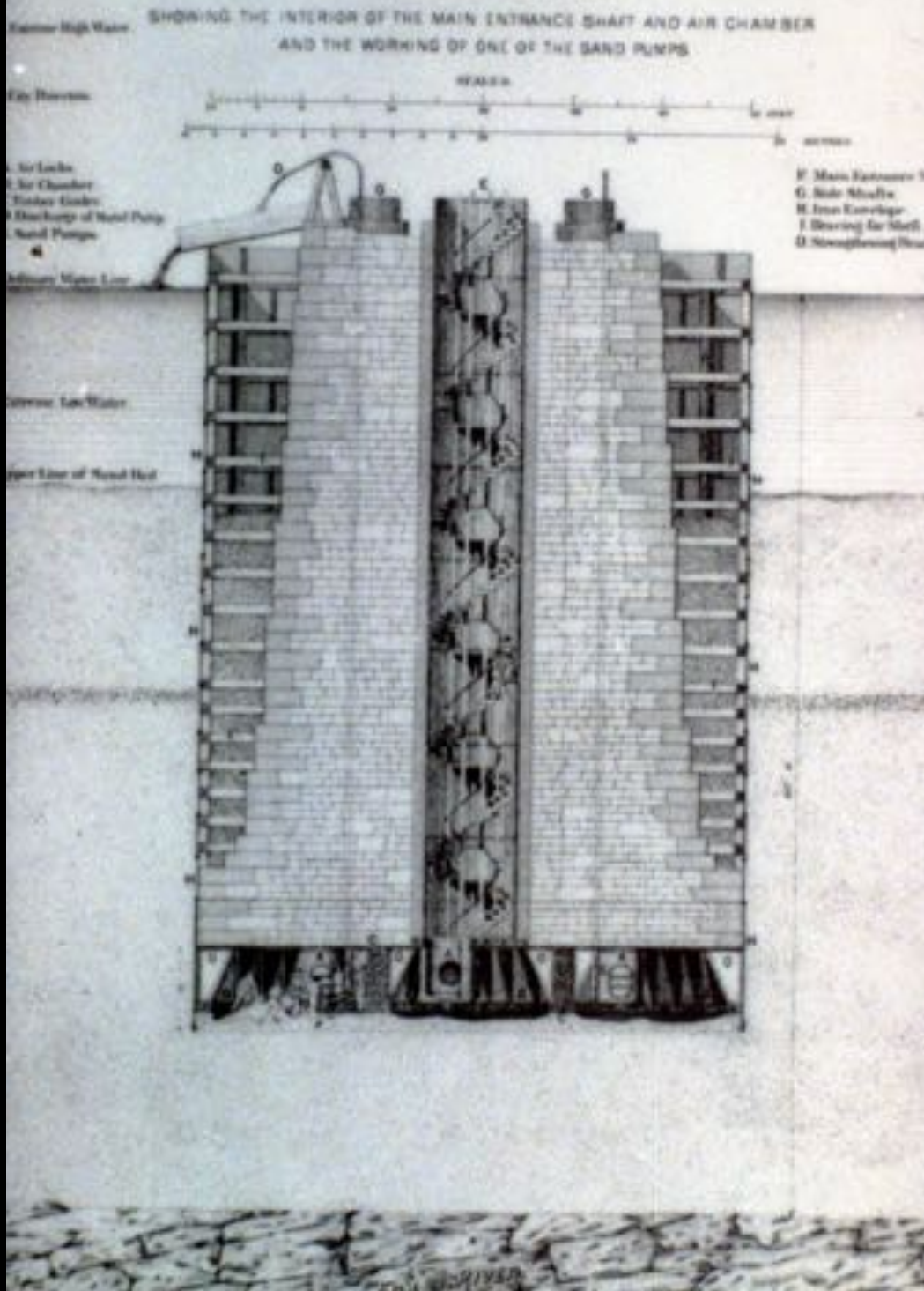


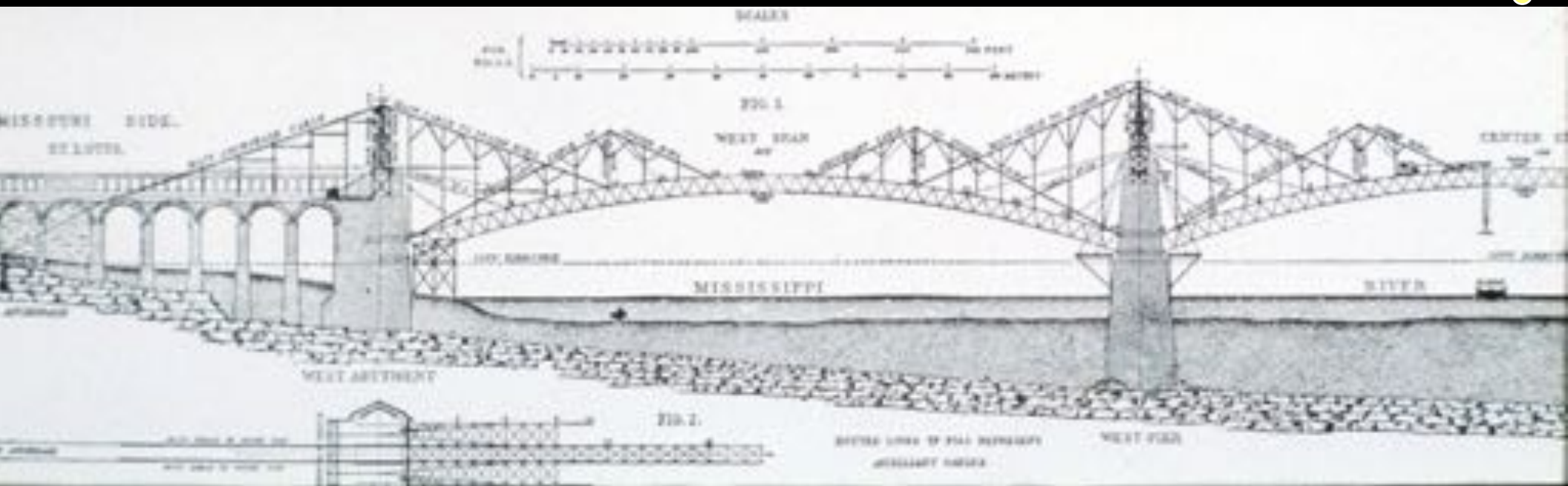




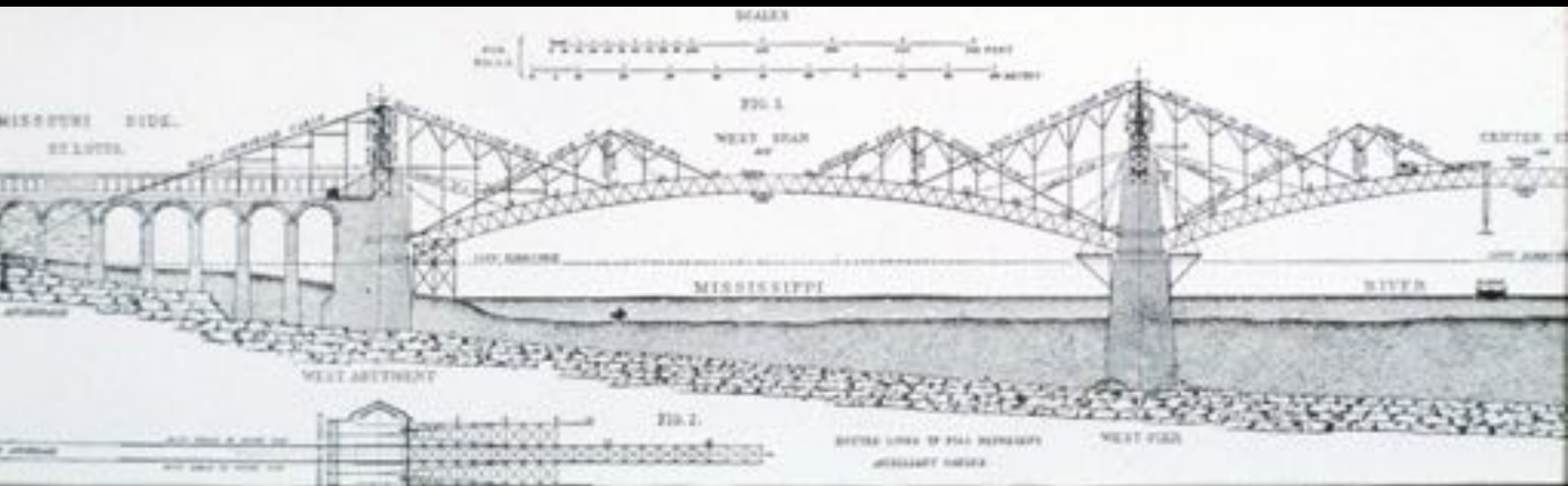
# SECTION OF EAST PIER AND CAISSON

ON LINE AB, PLATE VII.

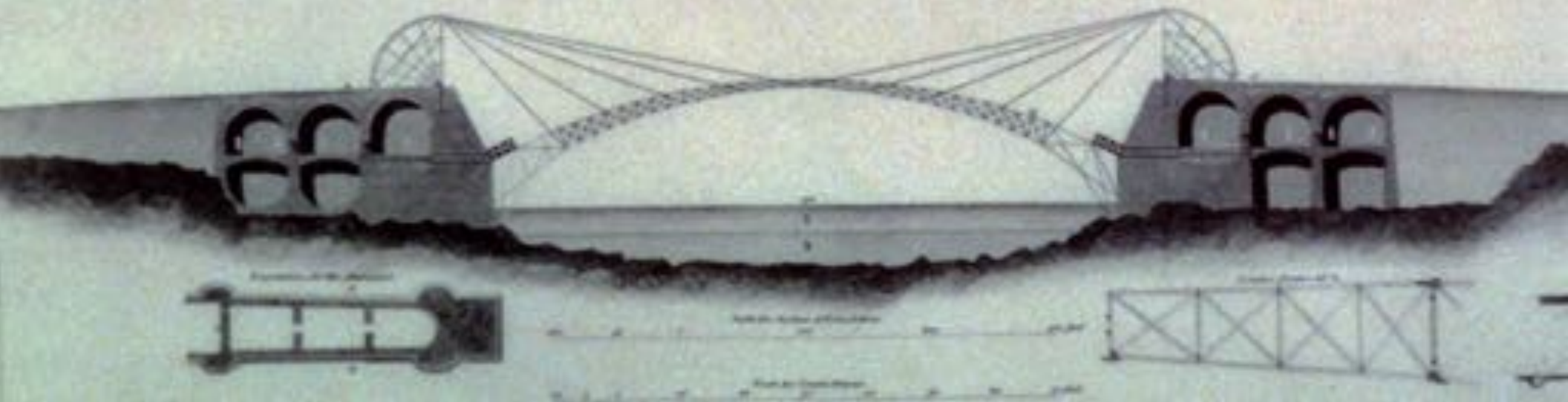


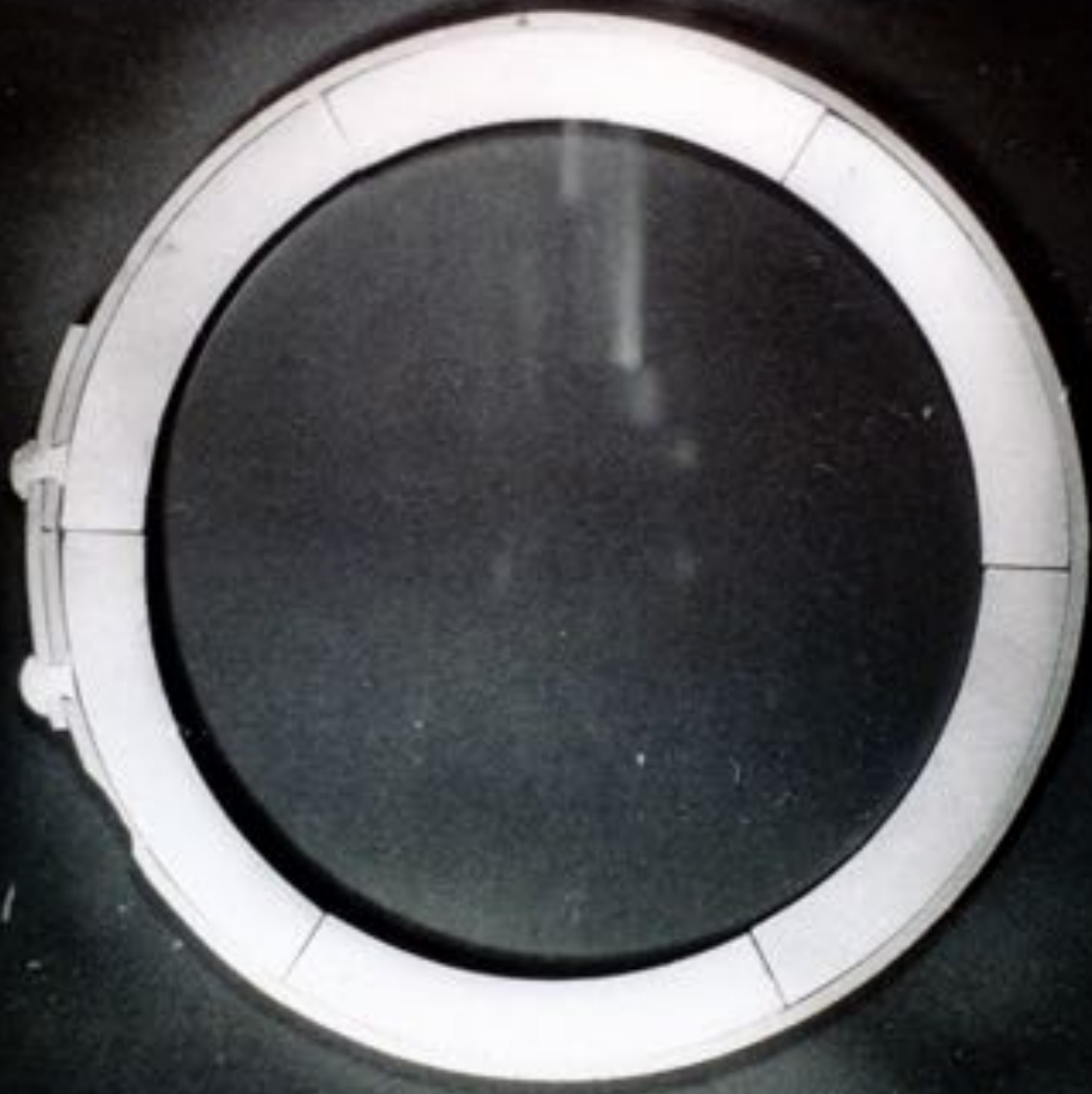




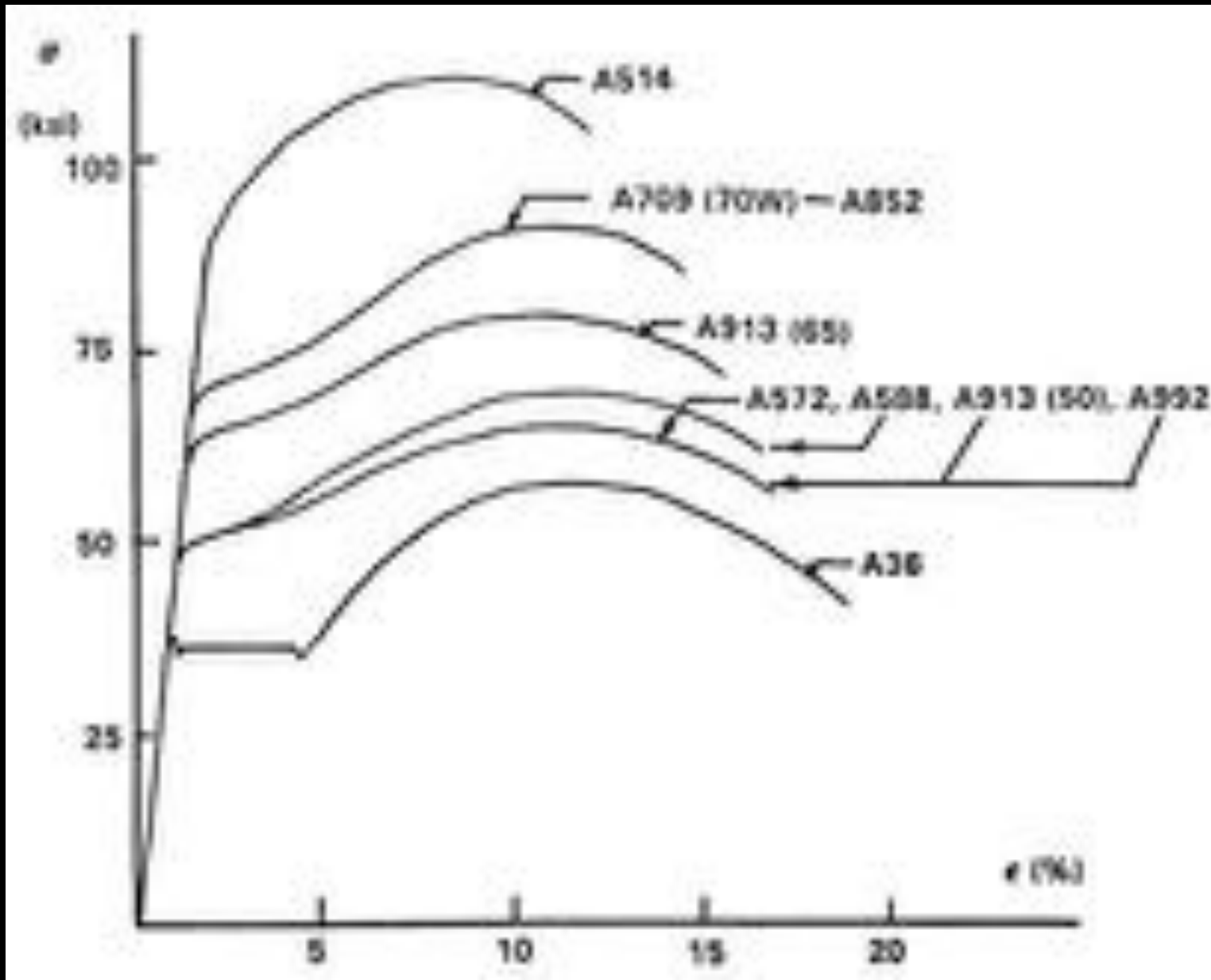


*DESIGN for the SUSPENDED CENTRONS for the proposed 1867 ARCH over the MISSISSIPPI RIVER.*



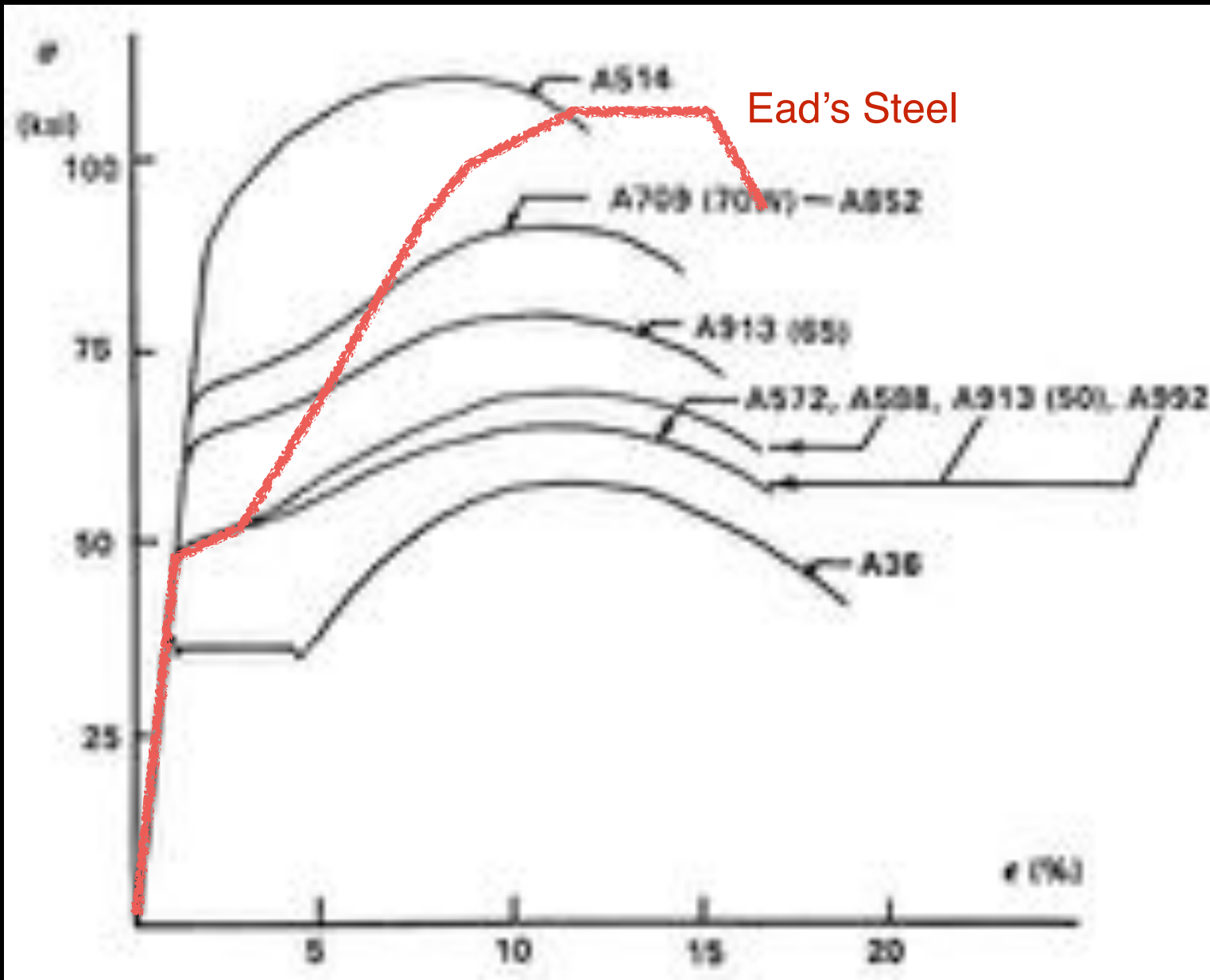


related to force when pulled



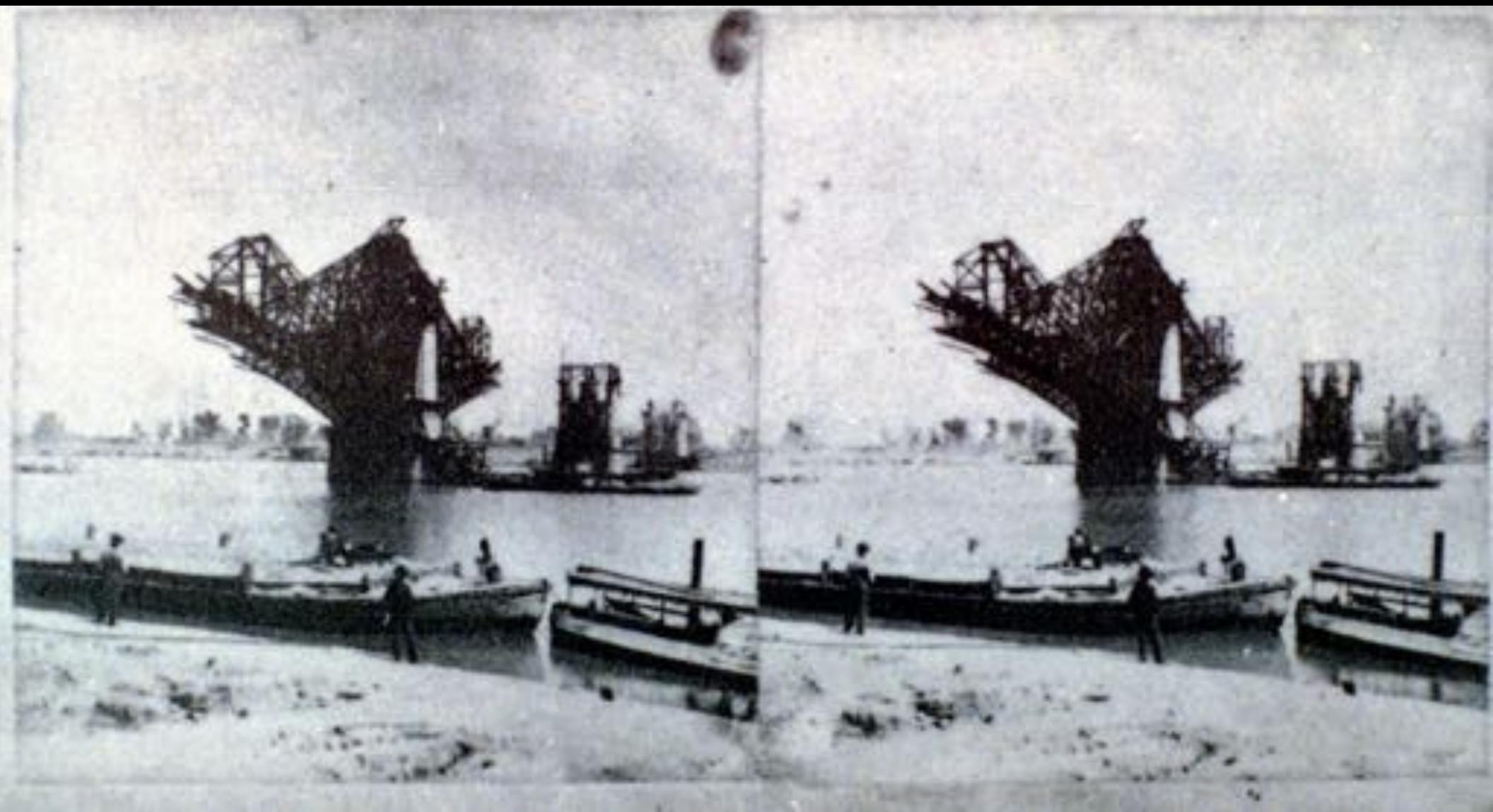
related to amount stretched

related to force when pulled



related to amount stretched





Eads Bridge - Dec. 1873



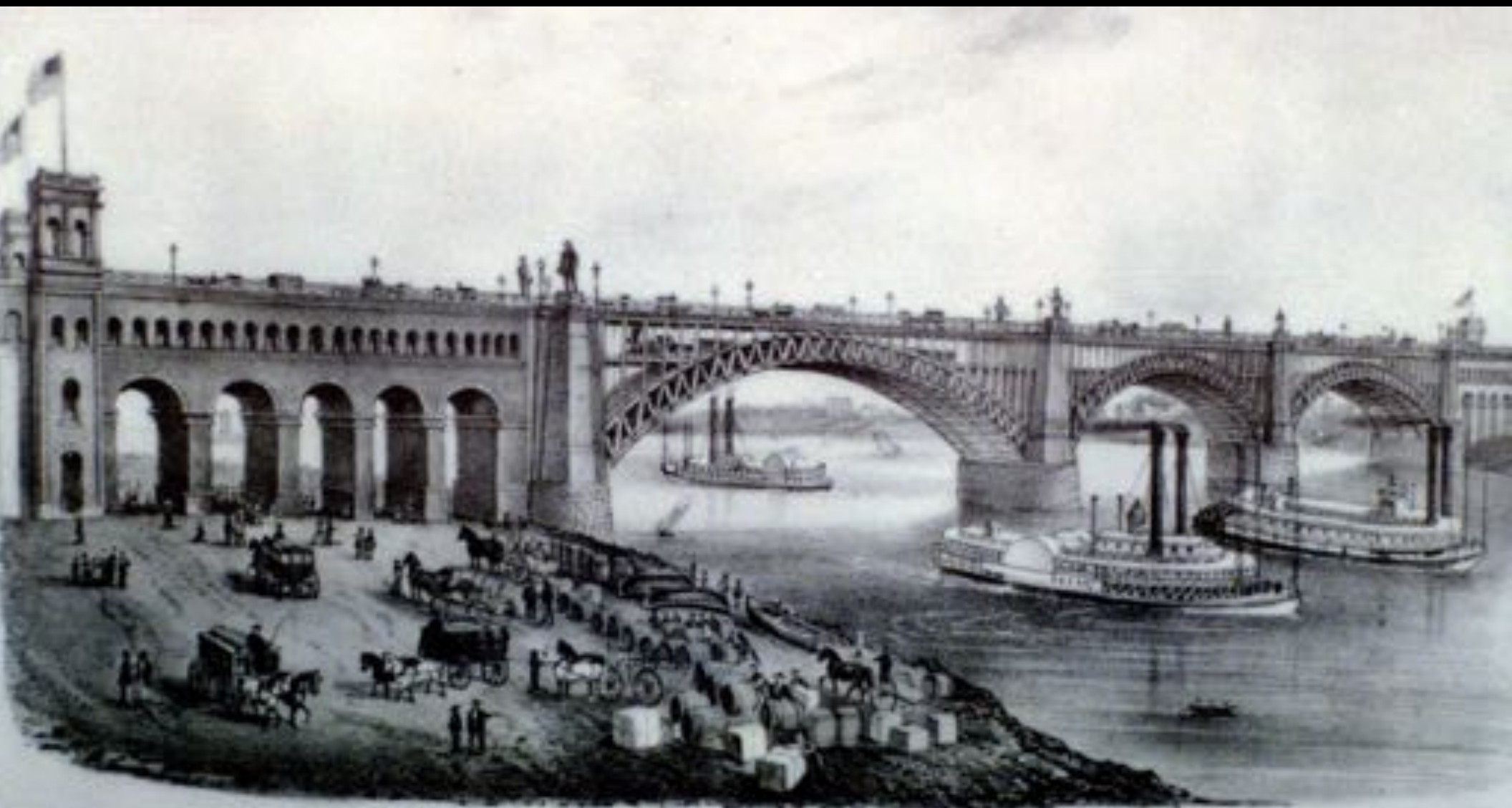


Eads Bridge - Jan. 1874









THE GREAT ST. LOUIS BRIDGE.  
ACROSS THE MISSISSIPPI RIVER.

The bridge was begun January 28th and  
the construction was completed in May 1874.  
The cost of the bridge was \$10,000,000.  
The bridge was the first of its kind  
in the world.

The bridge was the first of its kind  
in the world. It was the first of its kind  
in the world. It was the first of its kind  
in the world.

SAINT LOUIS

— THE —

Future Great City

OF THE

WORLD.

---

THIRD EDITION.

---

1871



Population of St. Louis in 1870, per United States census.....						812,963	
Population increased at the rate of 10 per cent per annum to 1880.....						811,742	
“	“	“	9	“	“	1890.....	1,917,571
“	“	“	6	“	“	1900.....	3,464,079
“	“	“	4	“	“	1910.....	5,083,297
“	“	“	3	“	“	1920.....	6,831,502
“	“	“	3	“	“	1930.....	9,180,967
“	“	“	2	“	“	1940.....	11,192,633
“	“	“	2	“	“	1950.....	13,643,757
“	“	“	1	“	“	1960.....	15,071,194
“	“	“	1	“	“	1970.....	16,647,941

2002 population of the metropolitan area is .....2,600,000



Dedication.

---

TO JAMES B. EADS,

THE MAN OF REAL GENIUS AND MARKED FIDELITY TO HIS FRIENDS,

THE CITIZEN OF GENUINE PATRIOTISM AND RARE PUBLIC

SPIRIT, THE MAN WORTHY OF HONOR

BECAUSE SELF-MADE,

THIS WORK,

DEVOTED TO THE FUTURE OF A CITY WHOSE

BEST HOPE IS IN SUCH MEN, IS

DEDICATED BY

THE AUTHOR.



July 4, 1874





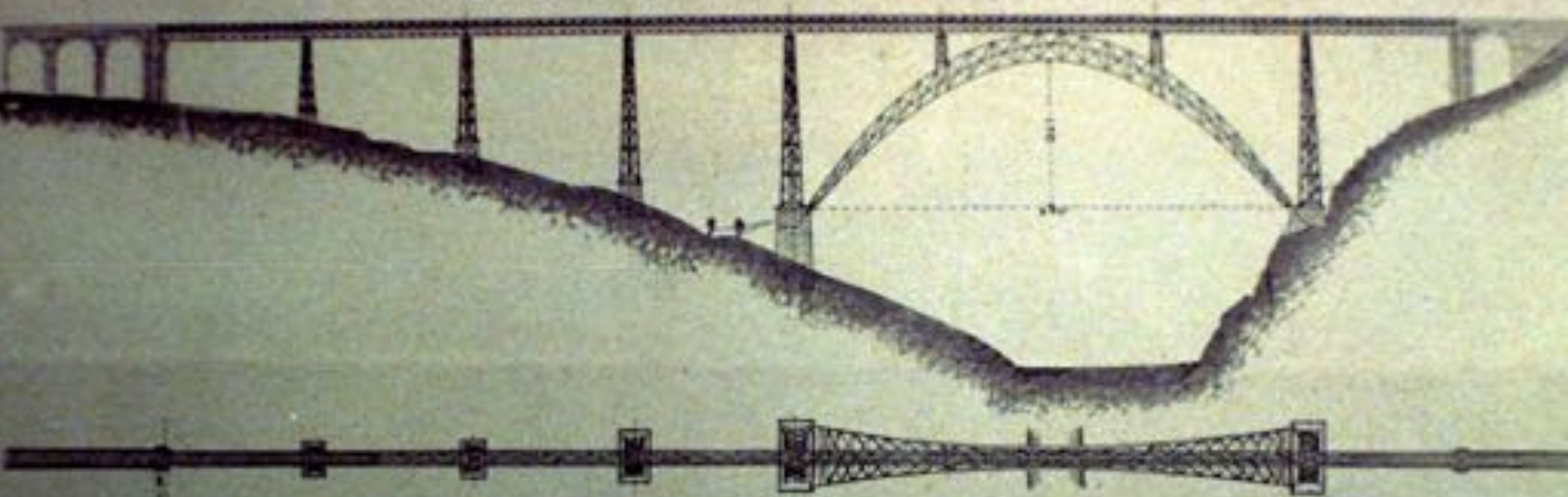




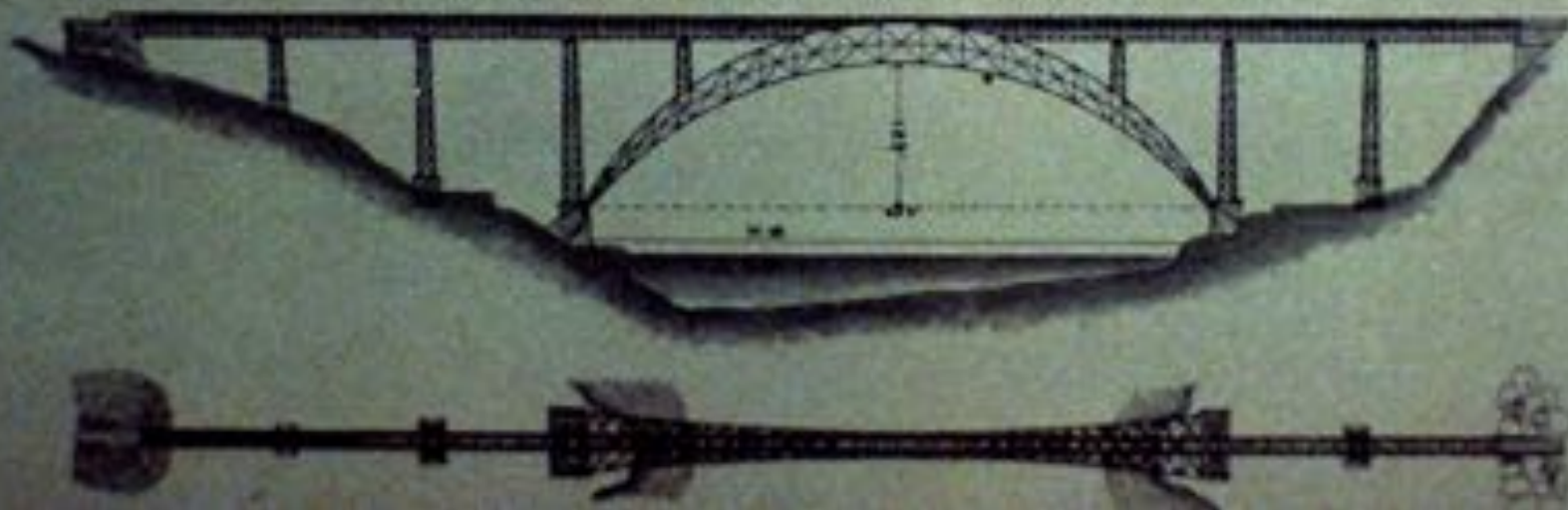




THE GARABIT VIADUCT OVER THE TRUYERE, CENTRAL FRANCE.



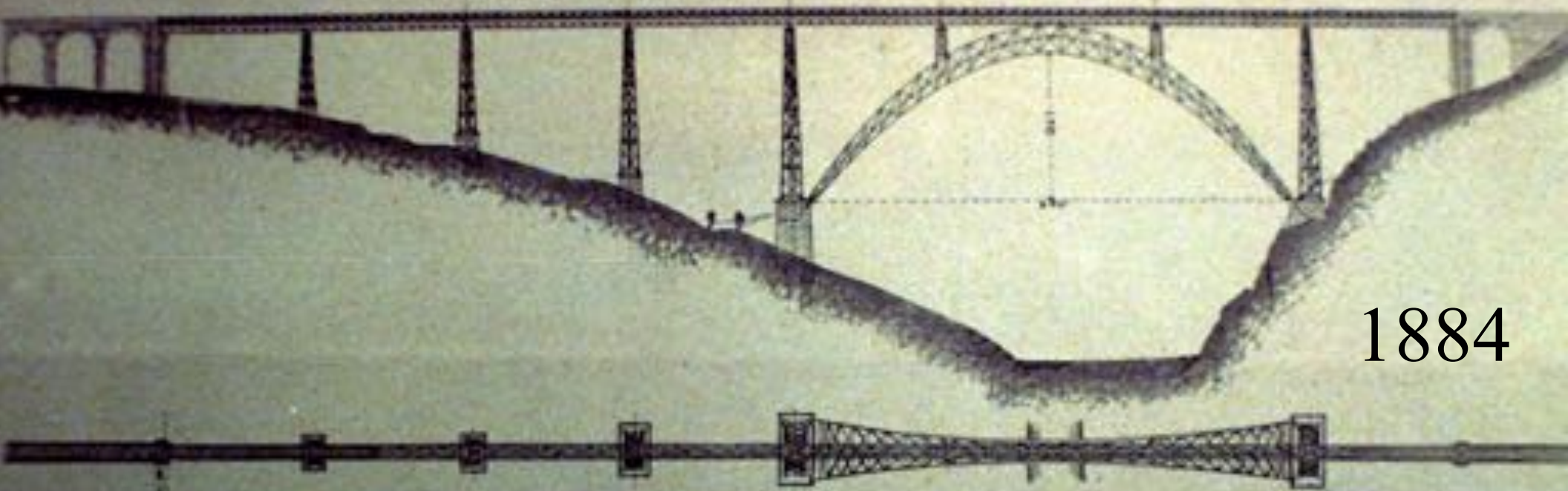
PIA MARIA BRIDGE OVER THE BOURG, OPORTO, PORTUGAL.



Can you identify differences?

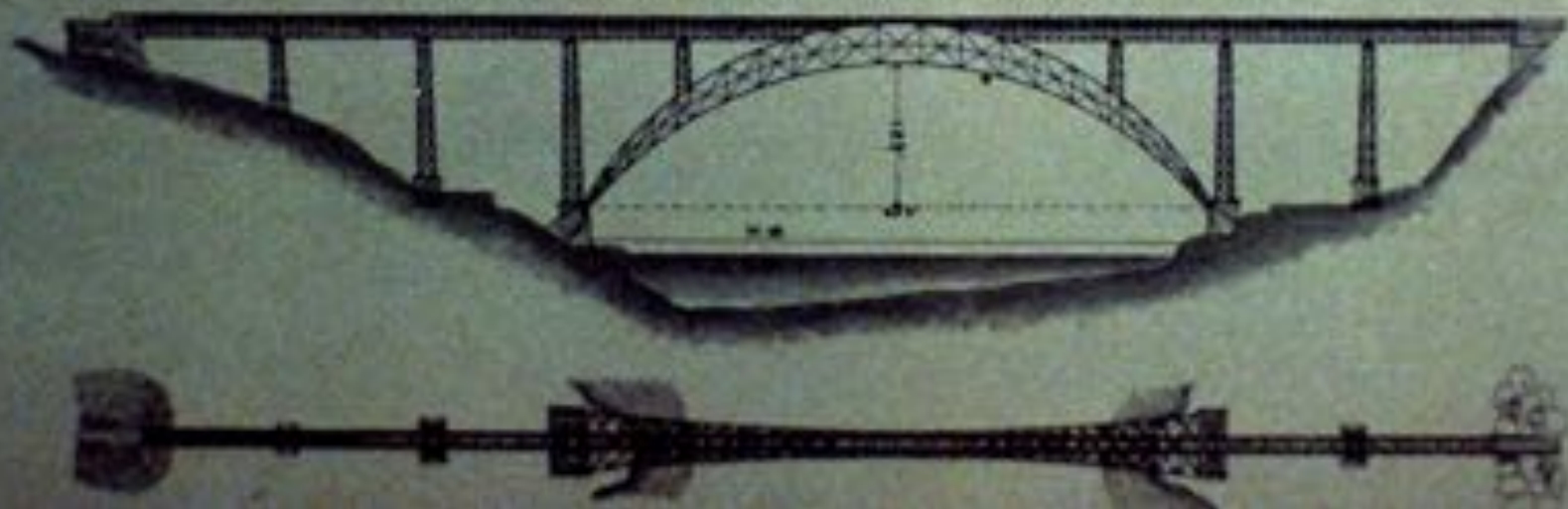


THE GARABIT VIADUCT OVER THE TRUYERE, CENTRAL FRANCE.



1884

PIA MARIA BRIDGE OVER THE BOURG, OPORTO, PORTUGAL.



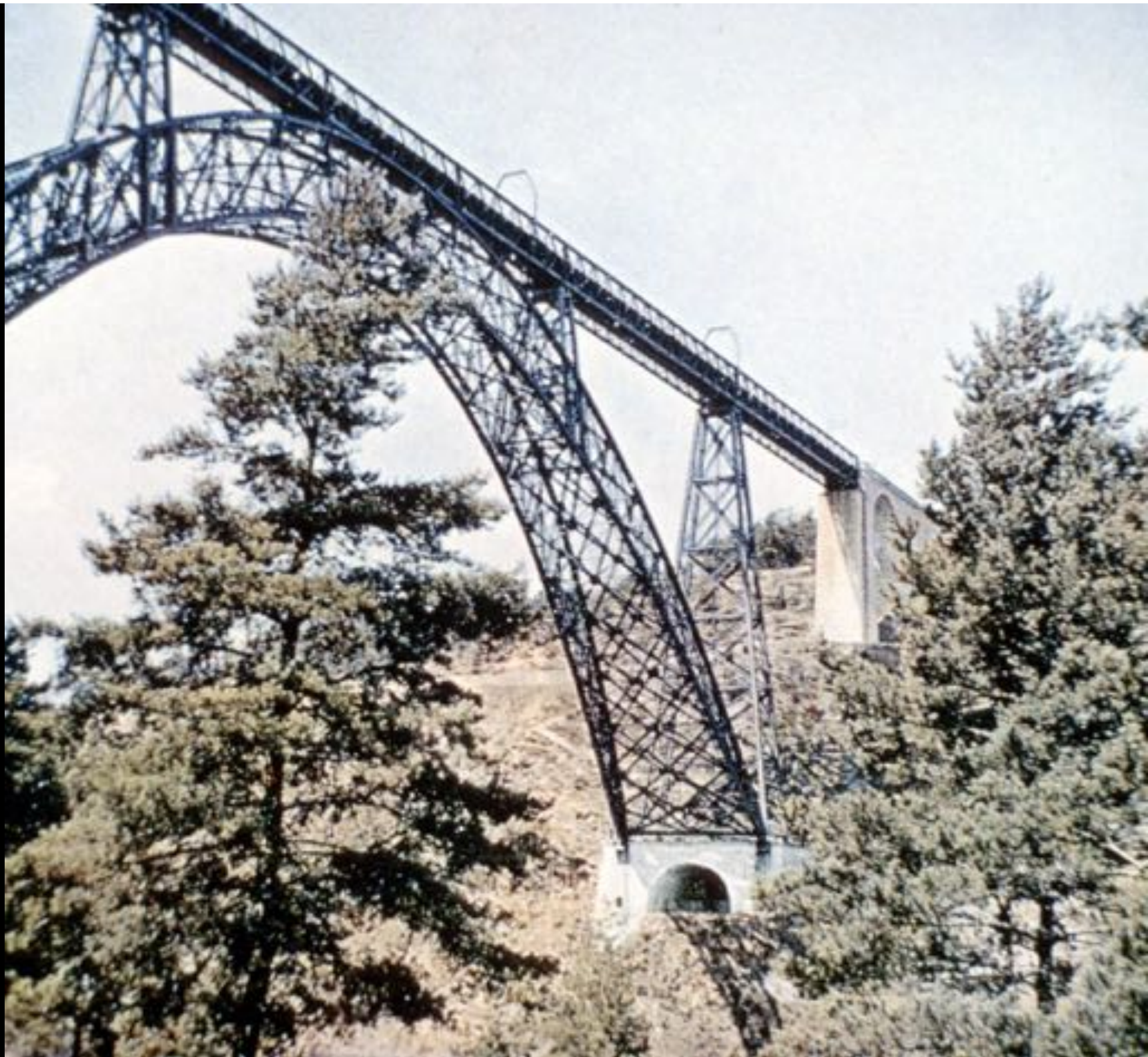
1877











Garabit  
Viaduct  
1884  
540 feet

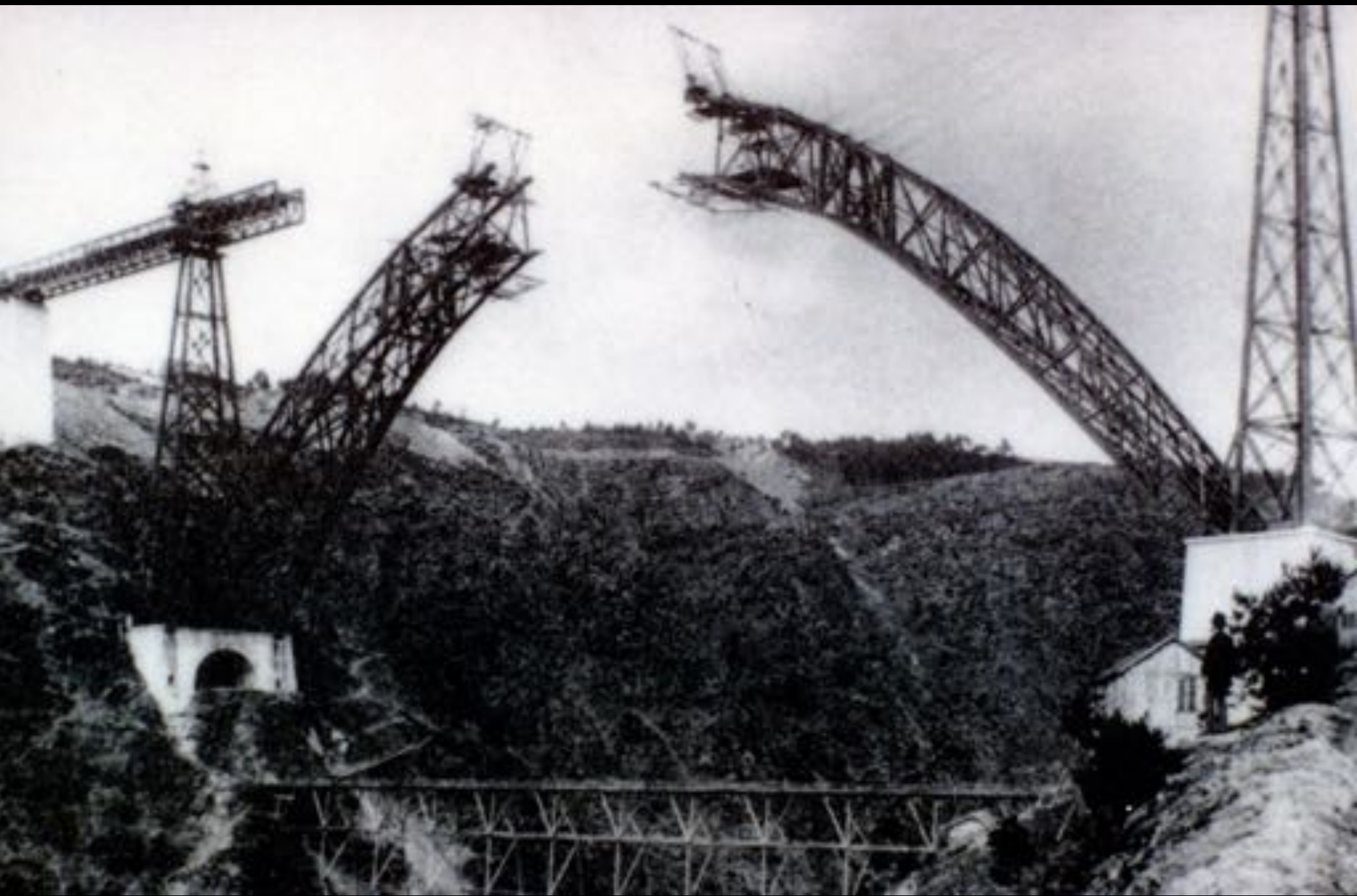


















Koblenz



Eads



Pia Maria



Garabit

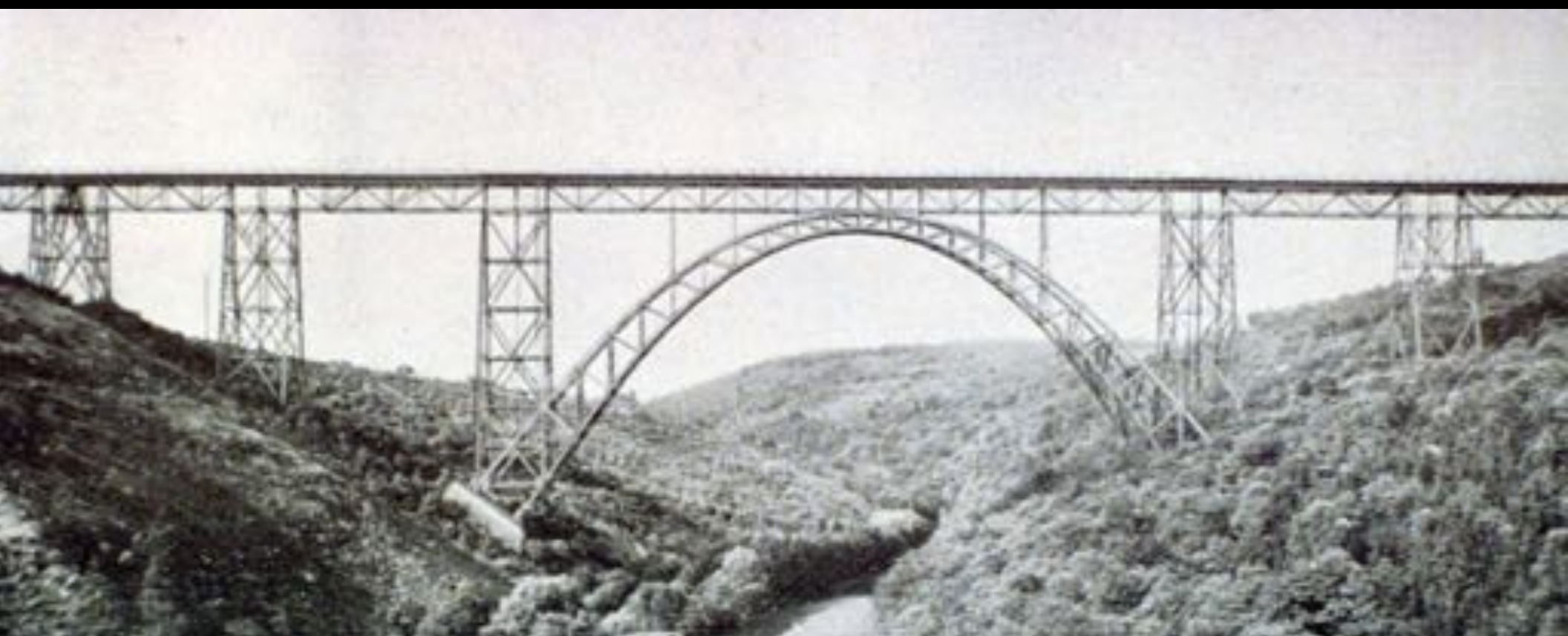




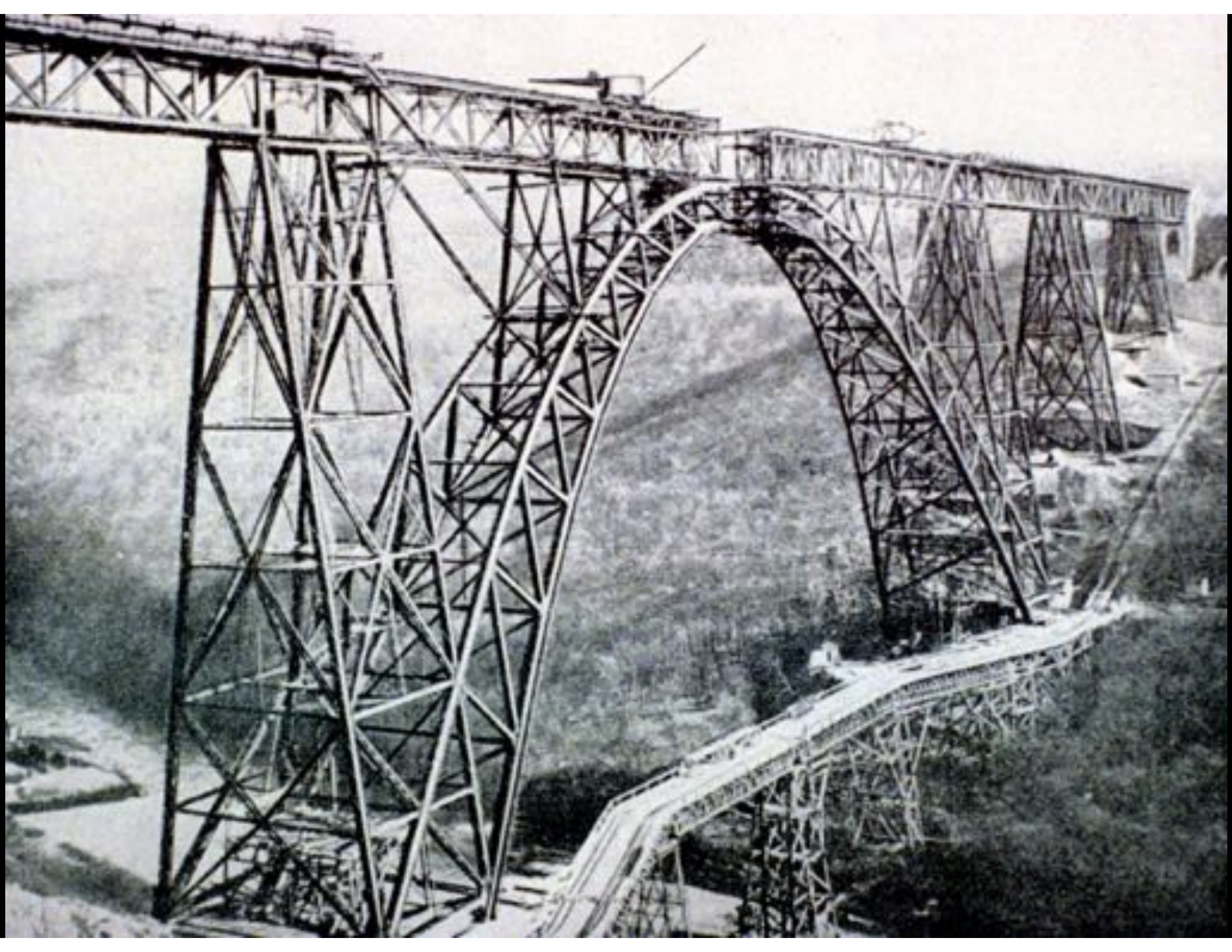
<http://www.structurae.de/en/photos/img3815.php>

Garabit Viaduct.

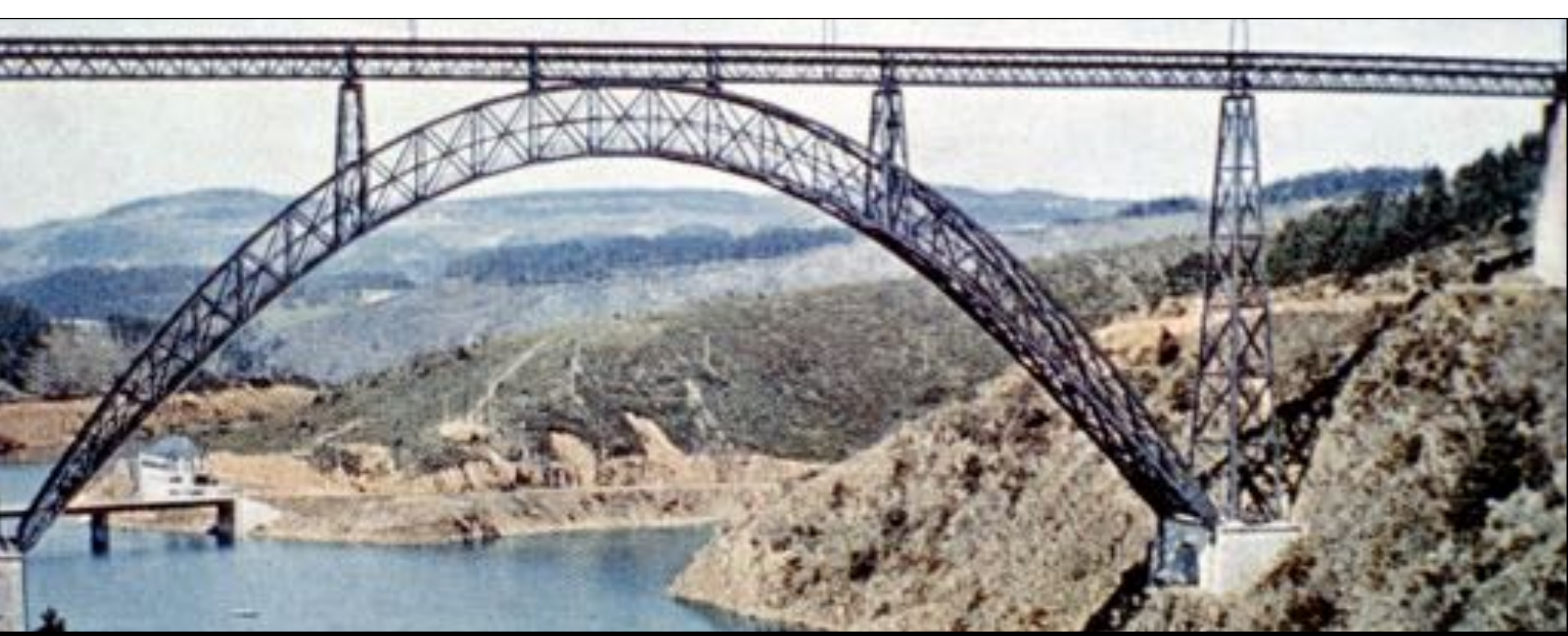
Photo by Jacques Mossot











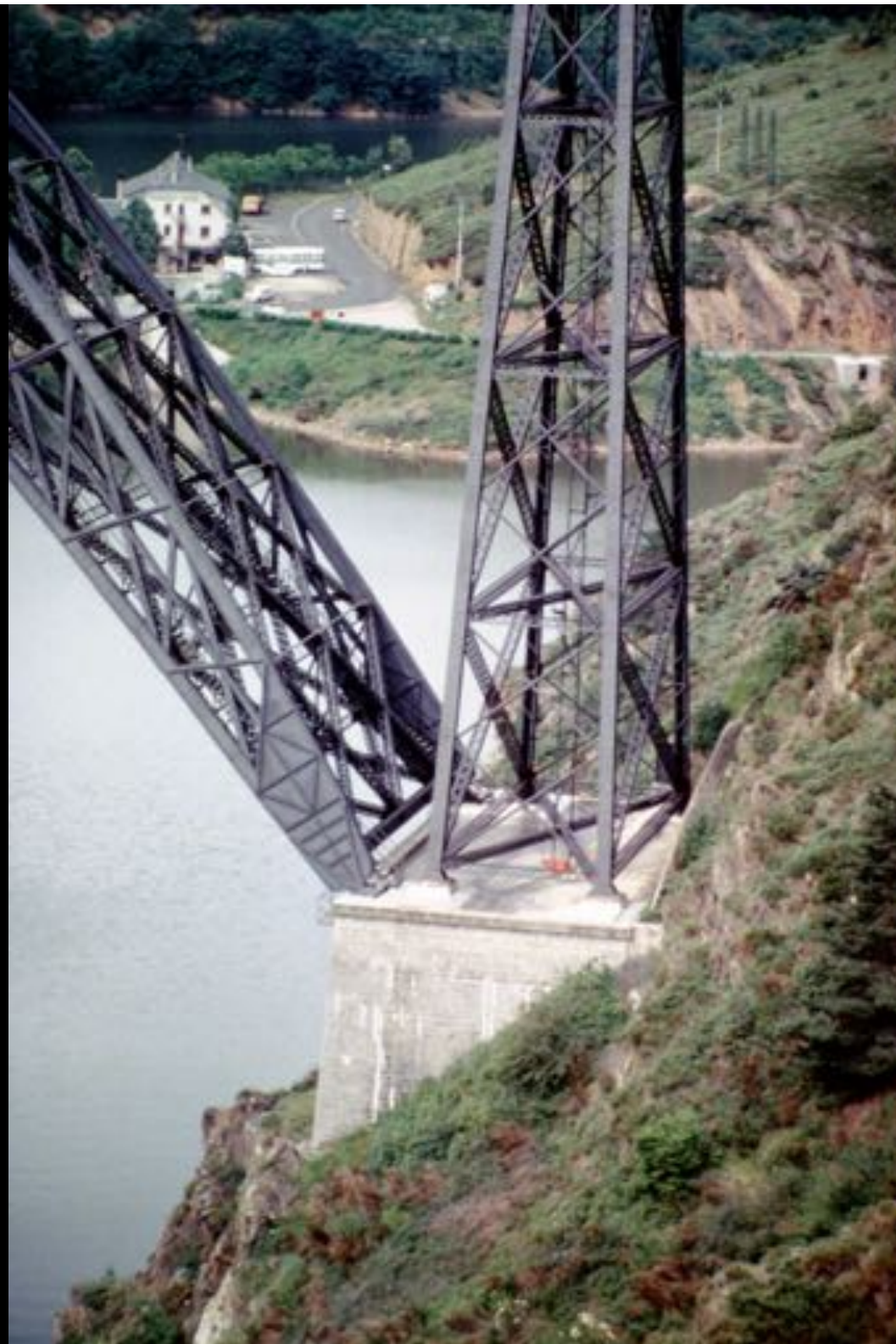


*Garabit*

A road sign with the word "Garabit" in a white serif font on a dark rectangular background. The sign is mounted on a metal post. In the background, a long viaduct with several tall pylons and arches spans across a valley. The landscape is green and hilly, with a white building visible on the right side of the valley. The sky is overcast.





















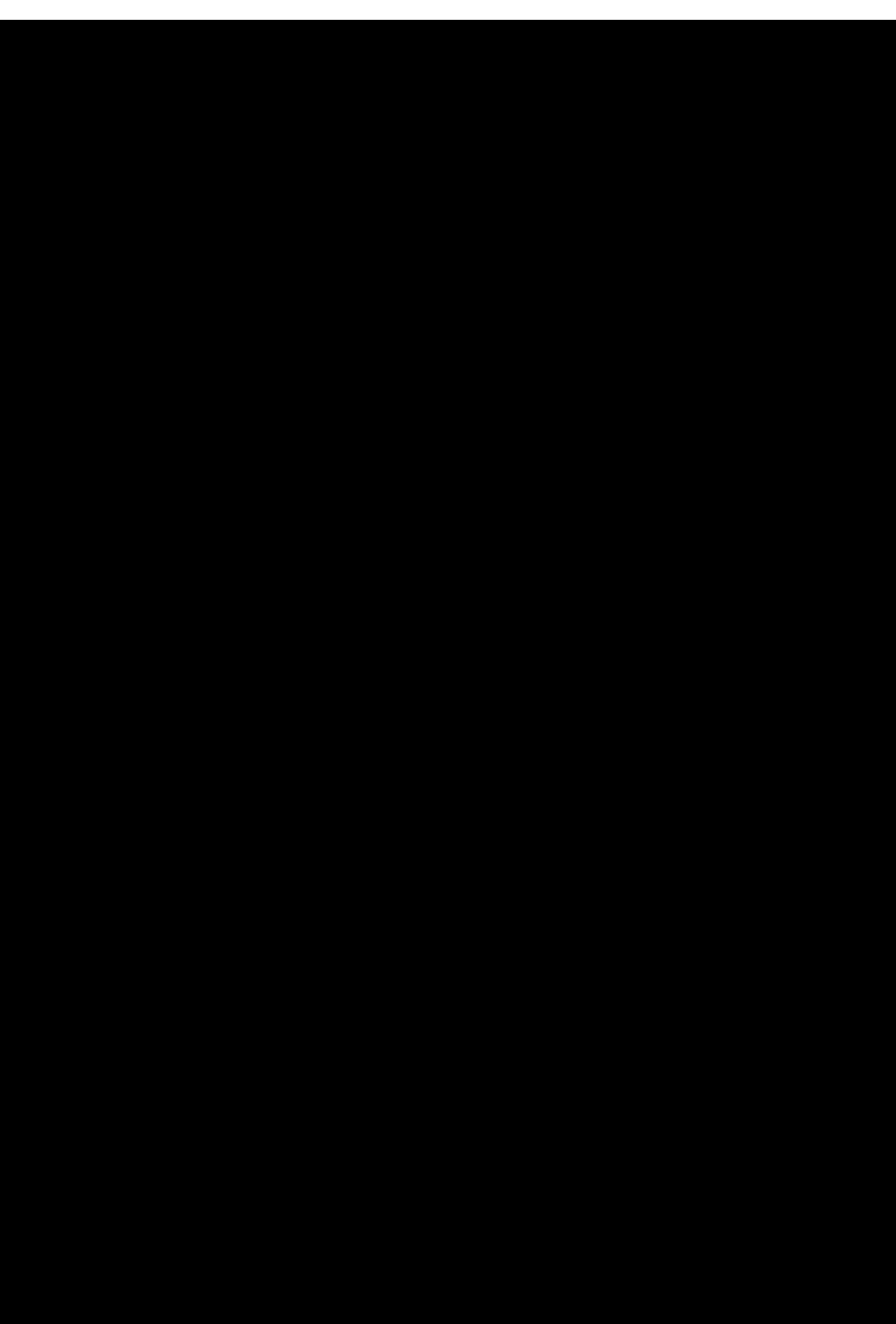
















PONT DE GARABIT  
*Designed by Eiffel the engineer.*

THE ENGINEER'S ÆSTHETIC  
AND  
ARCHITECTURE

Le Corbusier

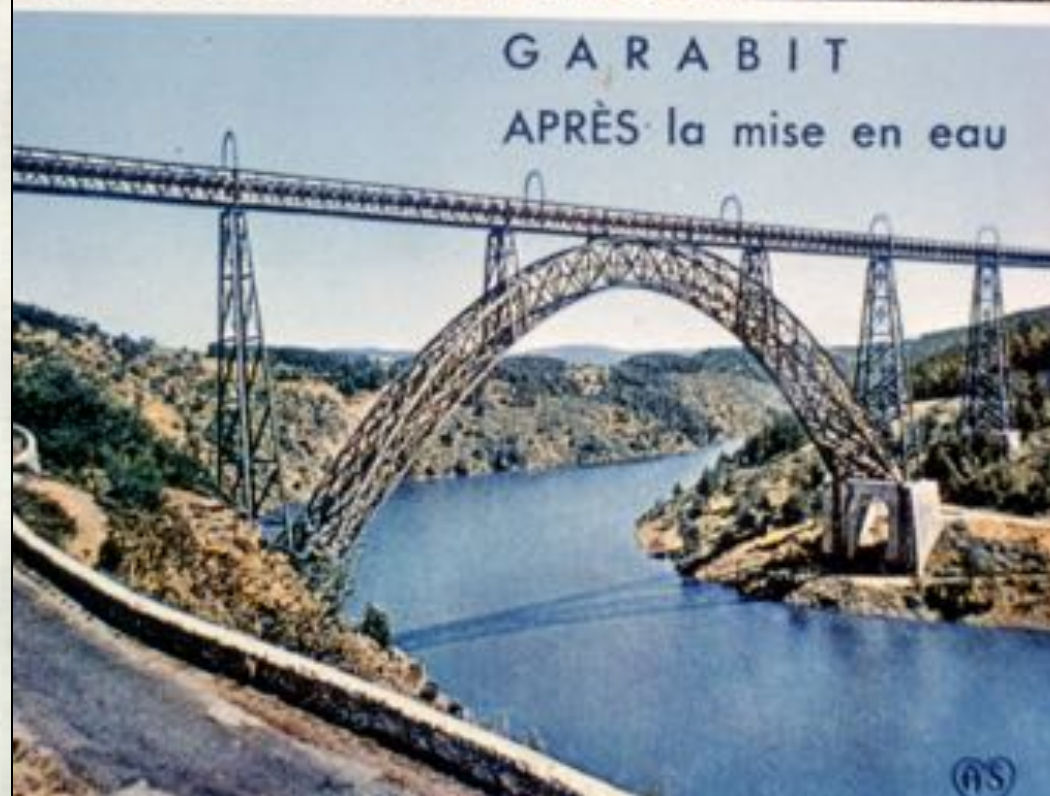






PONT DE GARABIT  
*Designed by Eiffel the engineer.*

THE ENGINEER'S ÆSTHETIC  
AND  
ARCHITECTURE







United Kingdom

Ireland

Netherlands

Belgium





**Firth of Tay**

**Firth of Forth**

**A**





1879, 75 people perished



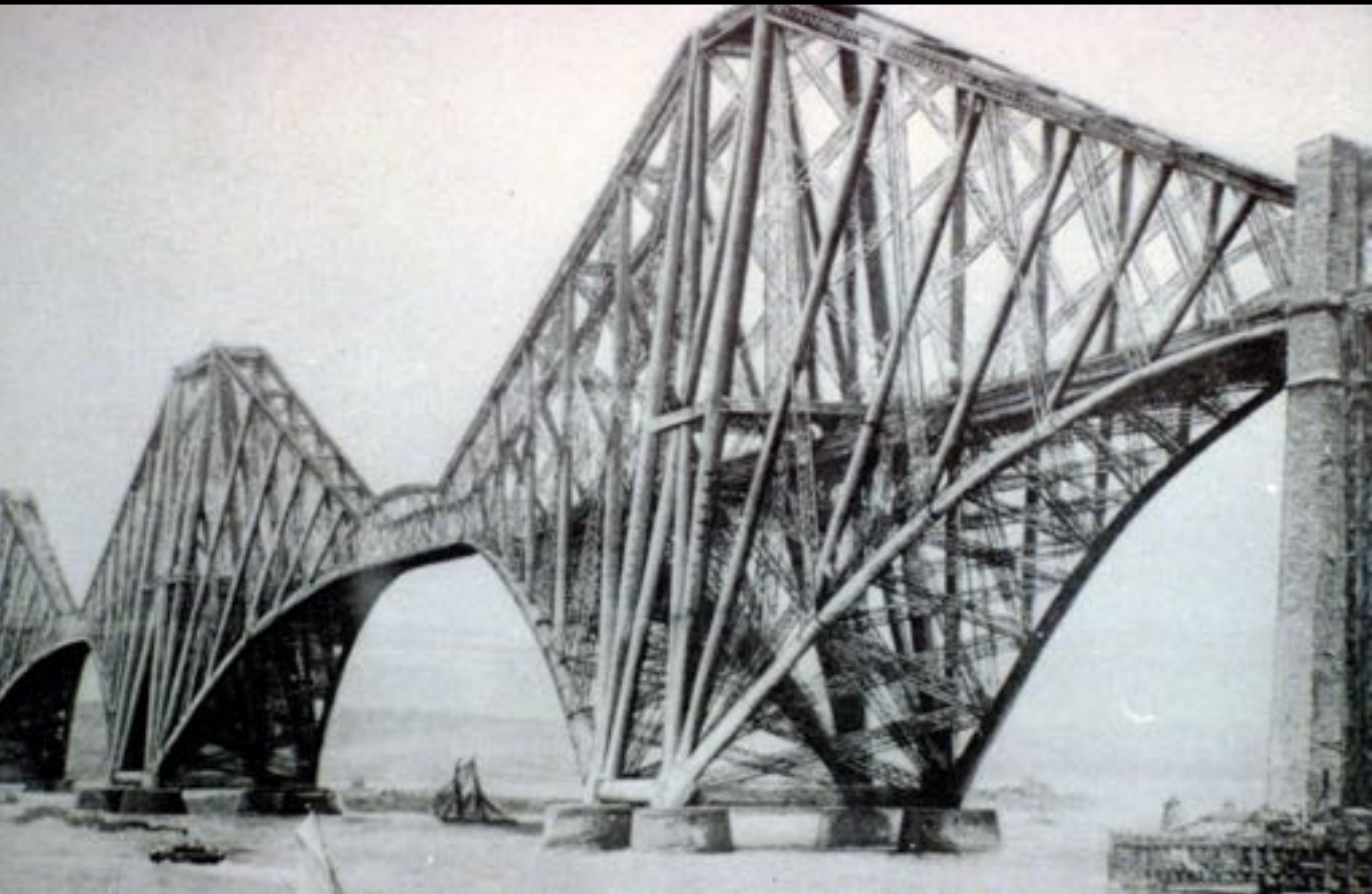
Court of inquiry proceedings, for Sir Thomas Bouch  
re: collapse of the Firth of Tay Br.

Q: Sir Thomas, did you in designing this bridge, make any allowance at all for wind pressure?

A: Not specially.

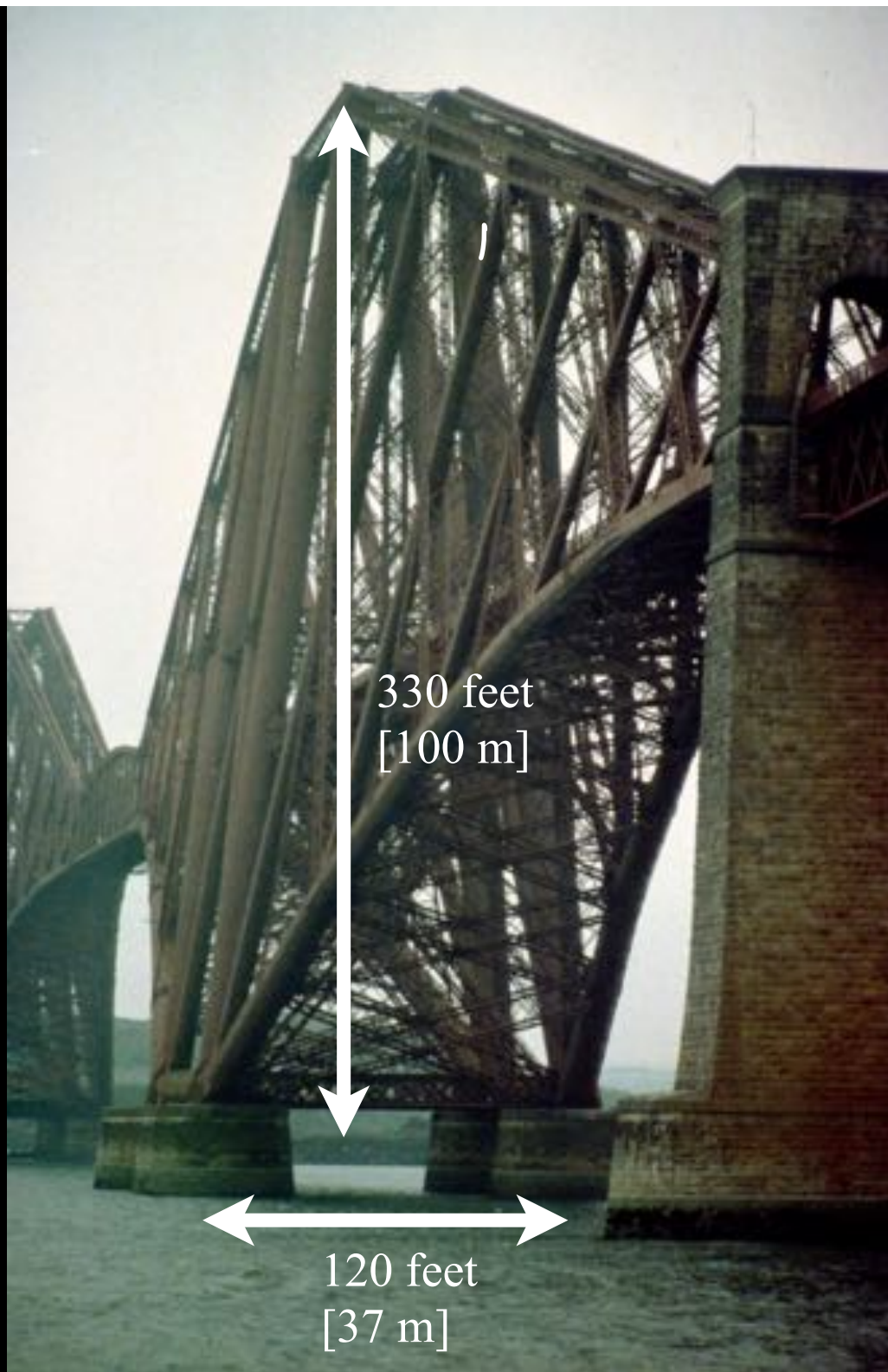
Q: You made no allowance?

A: Not specially.



Firth of Forth Bridge - Benjamin Baker - 1890 - 1710 ft [521 m]





330 feet  
[100 m]

120 feet  
[37 m]





# SCANNING THE FORTH BRIDGE

PO  
6052  
.E446  
S2  
1994  
c.1



*Poems by Robin Bell*

PETERLOO POETS

## *Scanning the Forth Bridge*

The bridge is wide. The Forth is deep.  
Iambic trains are made for sleep.

Trochee trains are bright achievers,  
sparkling through the cantilevers.

Dactylic trains cross the bridge very speedily,  
passengers munching their sandwiches greedily.

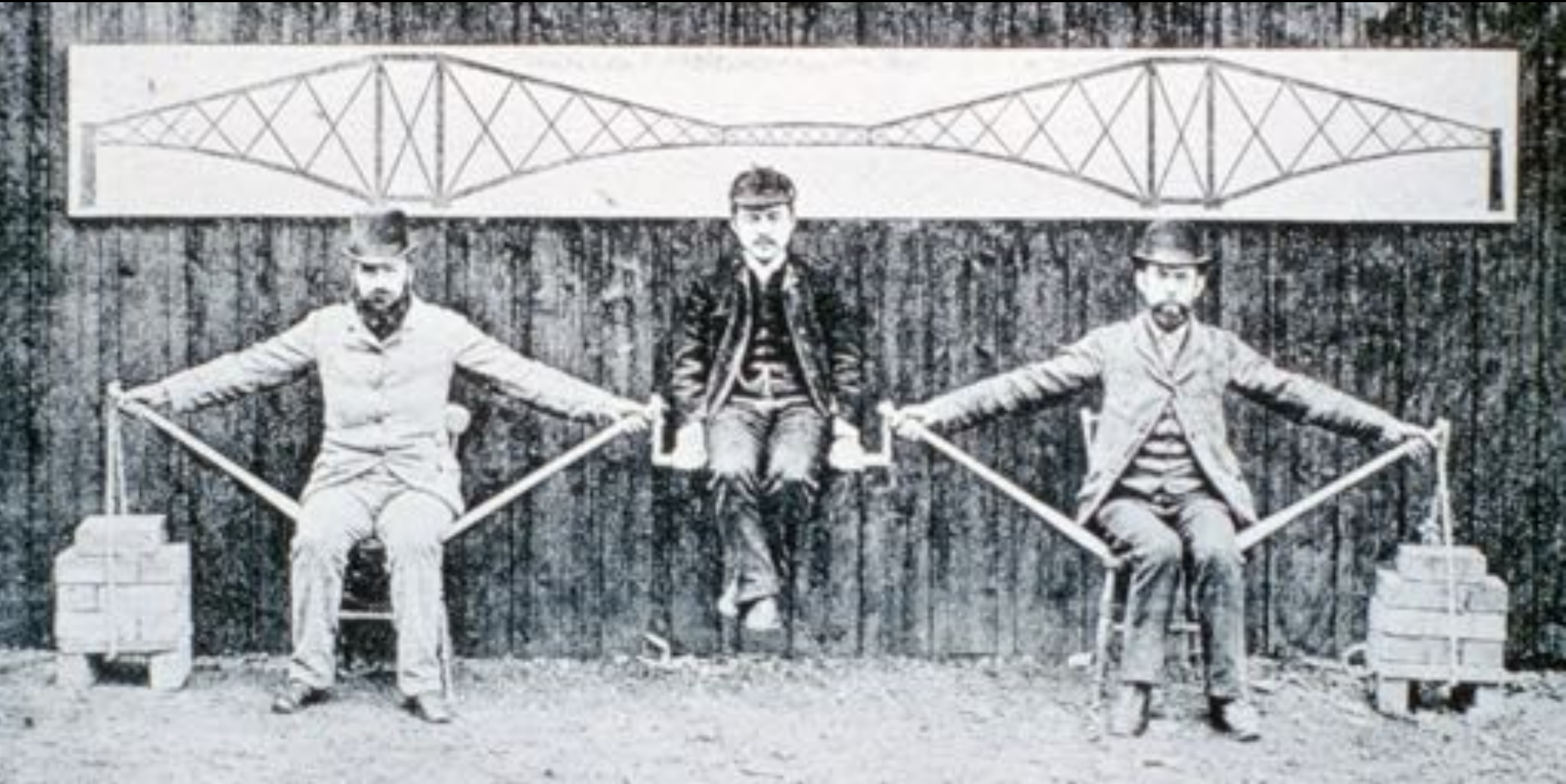
All the girders and seagulls and Anapaest trains  
can expect to get wet every time that it rains.

Spondee trains plod on, on, on, on.  
Dusk, dawn, dusk, dawn, yawn, yawn, yawn, yawn.

Workers work all year round: pots of paint, nuts and bolts.  
Cretic trains shake you up: nasty jars, sudden jolts.

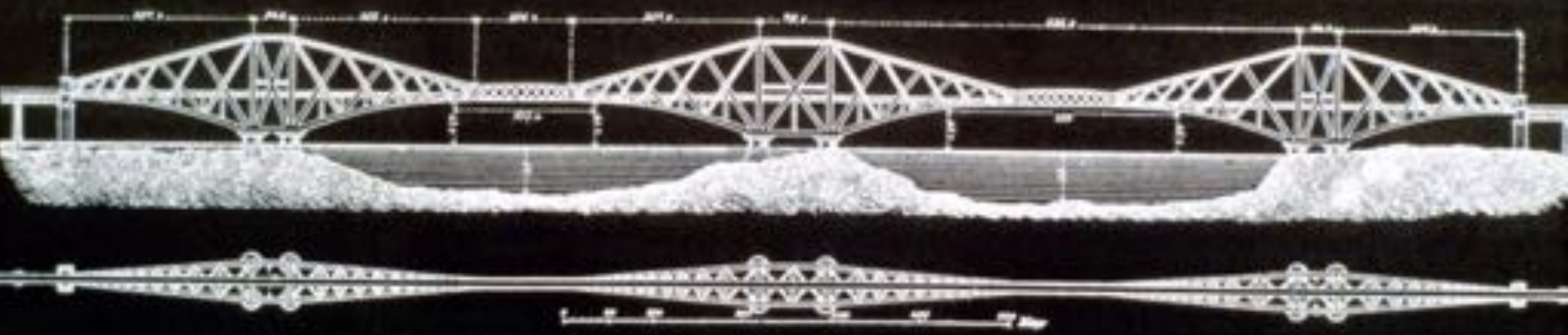
The Amphibrach trains travel swiftly but rarely,  
and say that the Dactyl's competing unfairly.

Of timid Pyrrhic trains  
not one remains.



can you identify tension and compression?























Social-Scientific-Symbolic

Eads Br.

Garabit Br.

Forth Br.

Economy-Efficiency-Elegance

# Eiffel Tower Structural Study

introduction to statics



# Tools and methods for structural analysis

Free body diagrams

Equilibrium

Load path

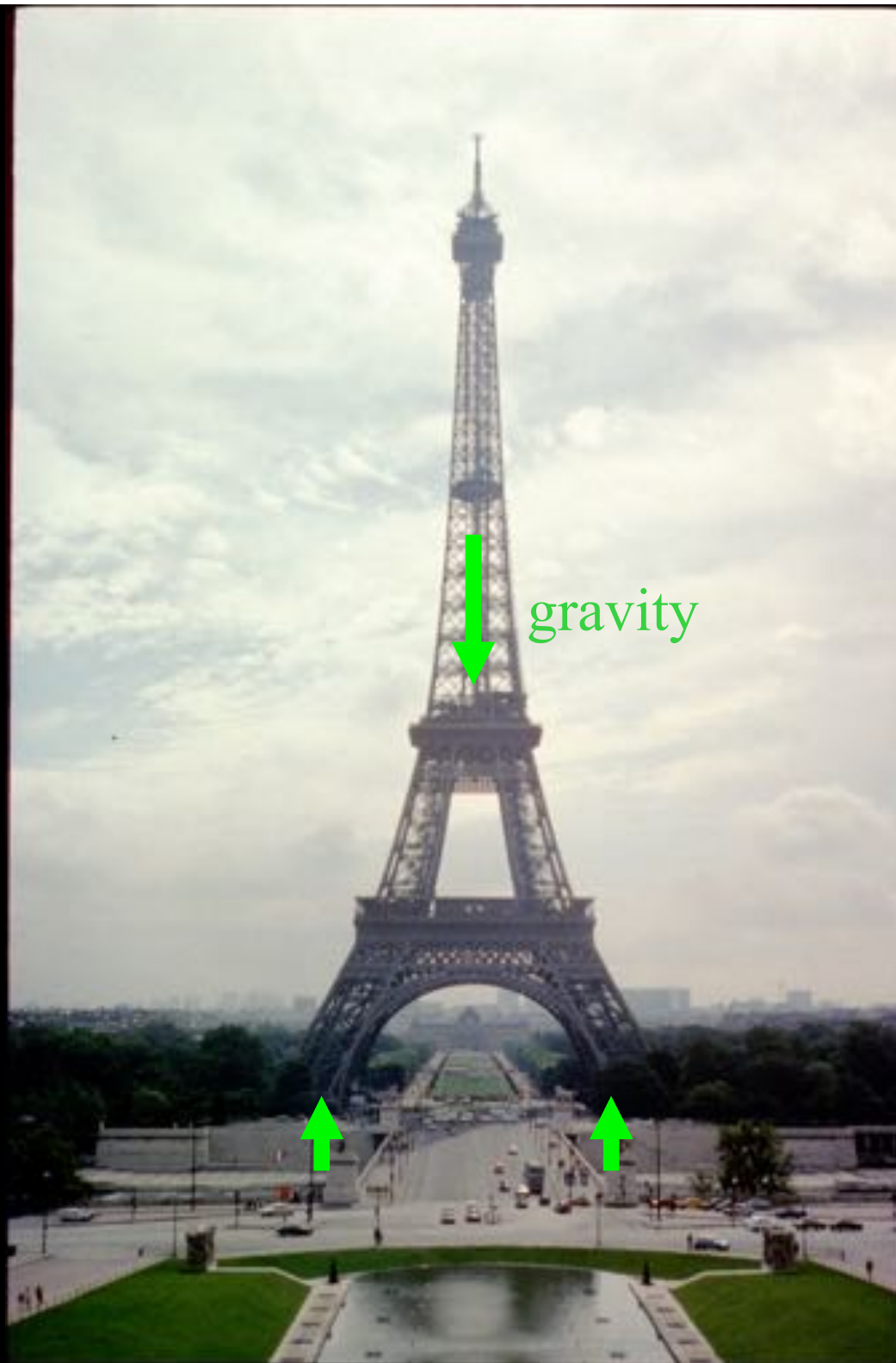
# Free Body Diagrams





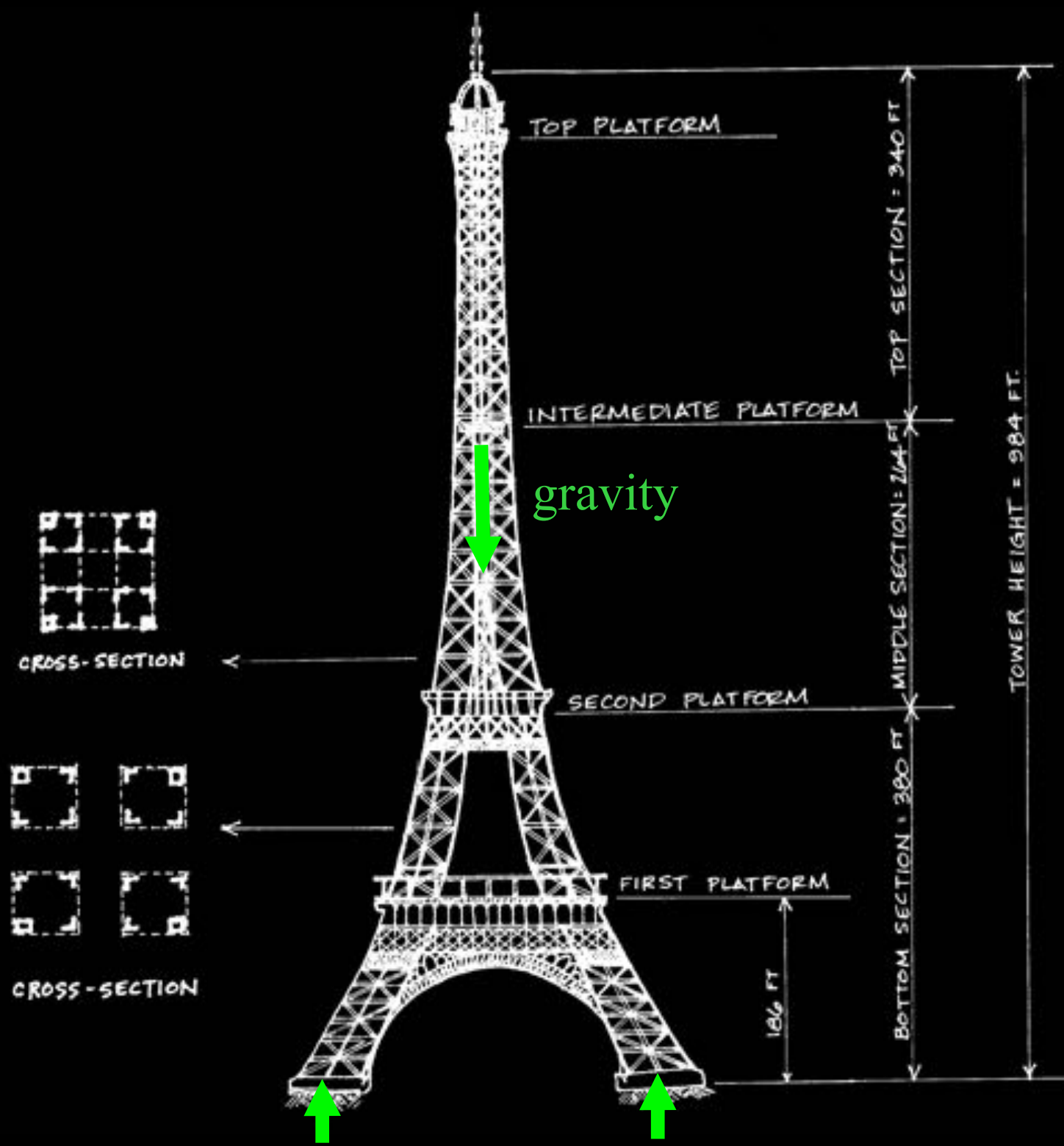


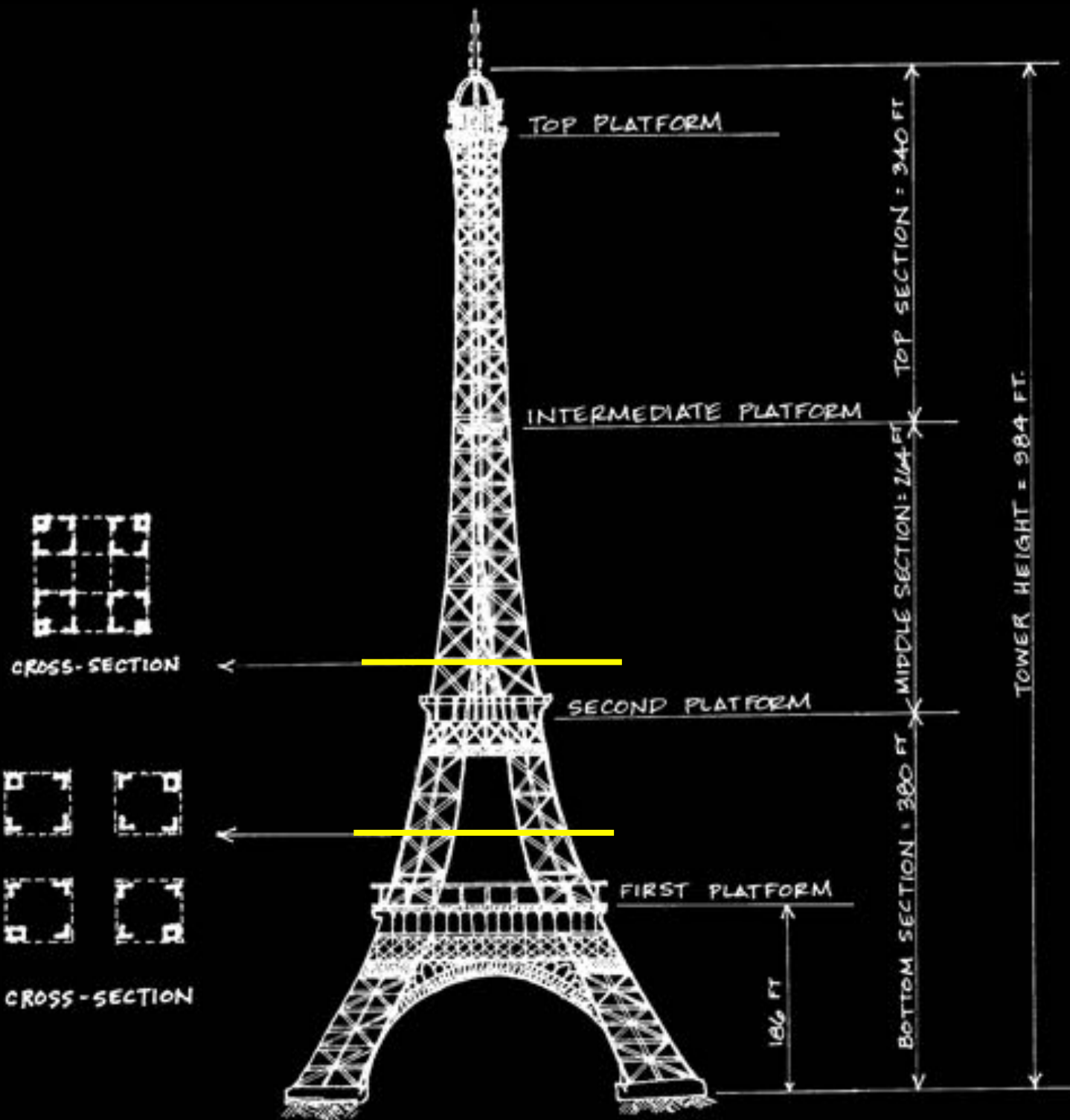
gravity

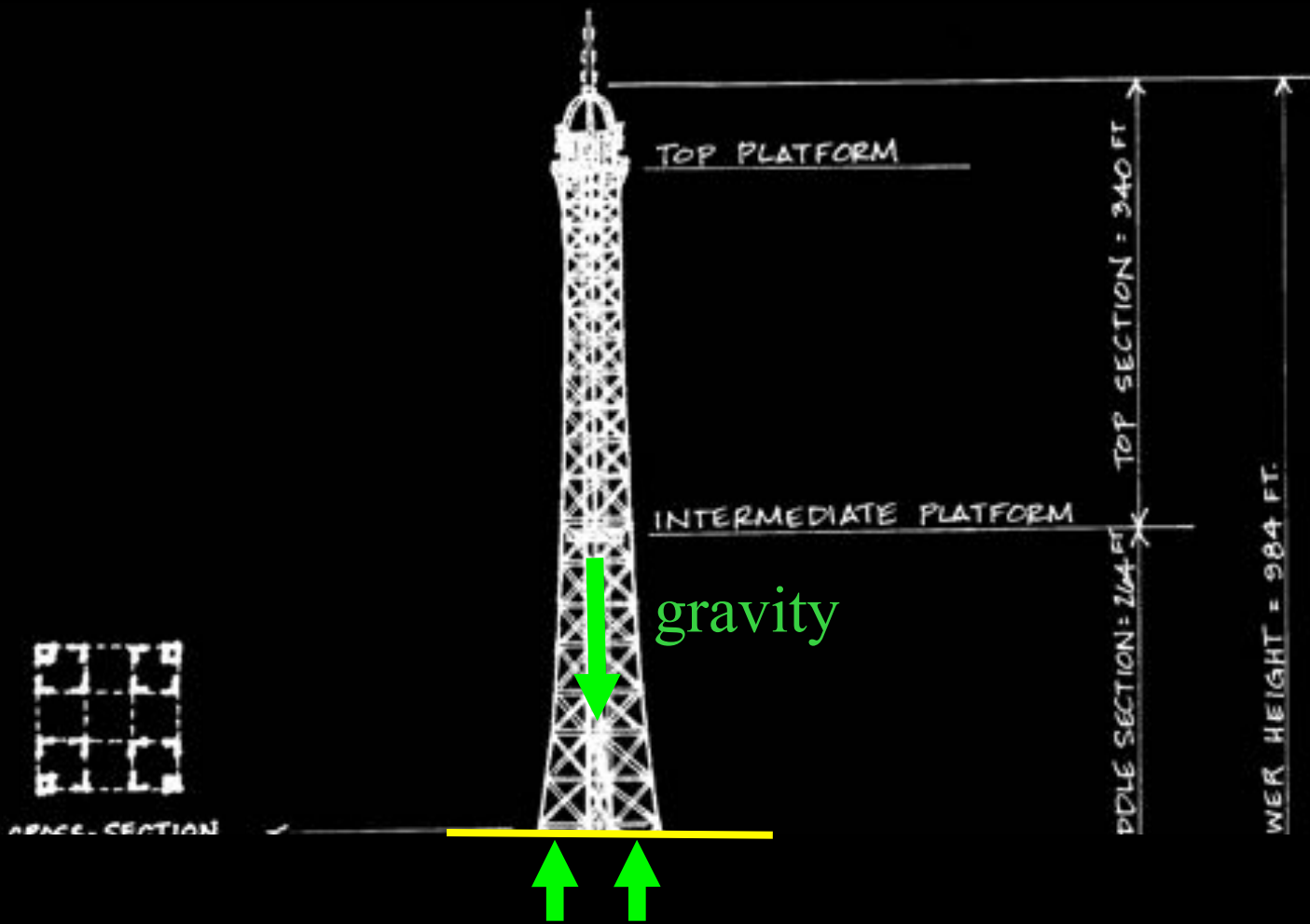


gravity

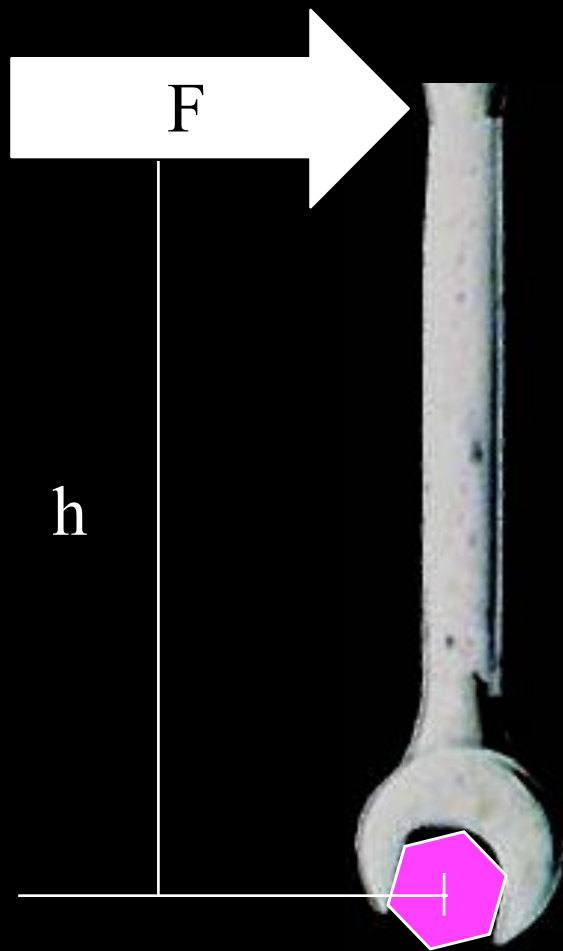






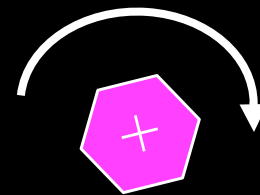


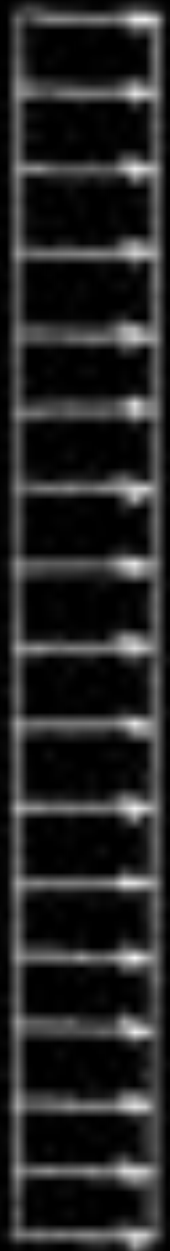




=

$$M = Fh$$



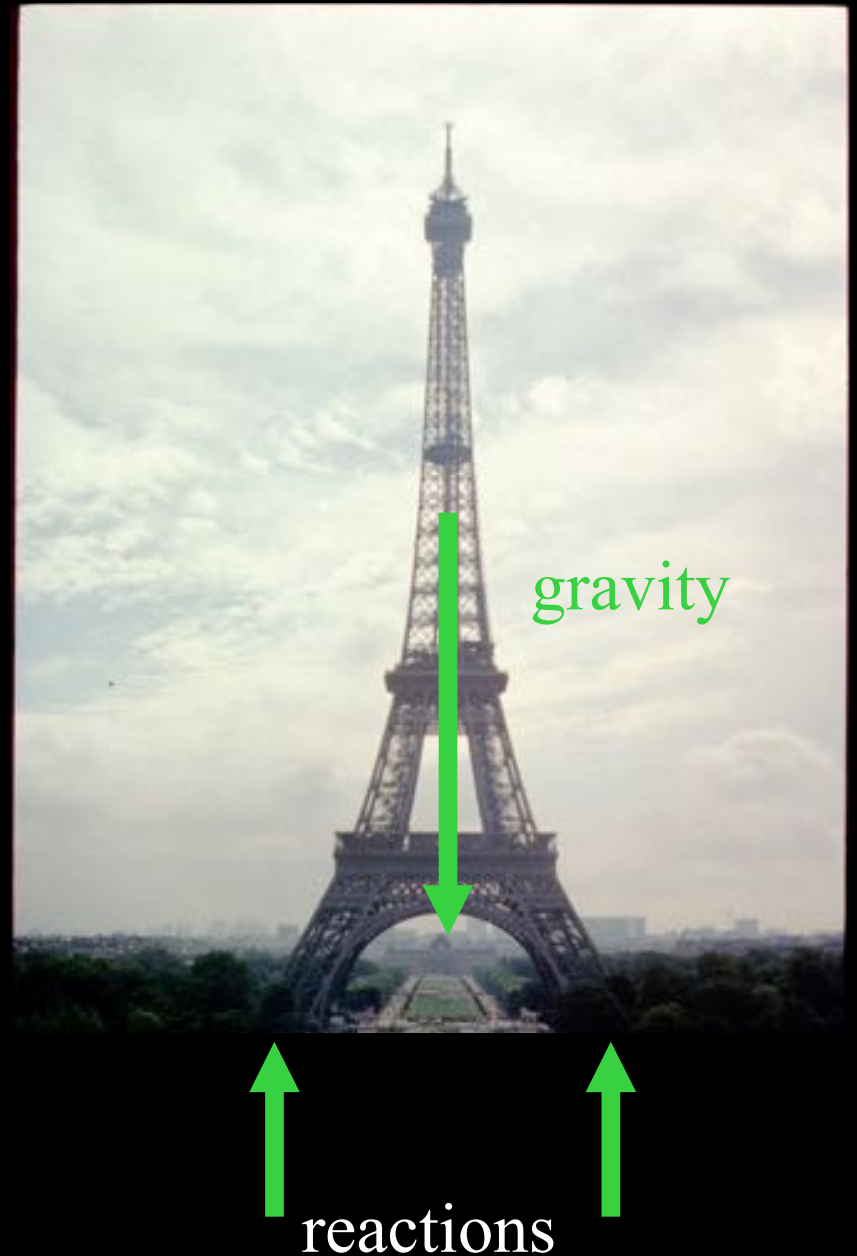


$p=2.6 \text{ k/ft}$

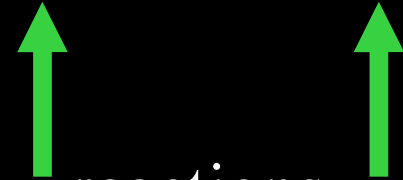
$$P = wH$$
$$P = (2.6)(984)$$
$$P = 2600 \text{ kips}$$



$H = 984 \text{ ft}$

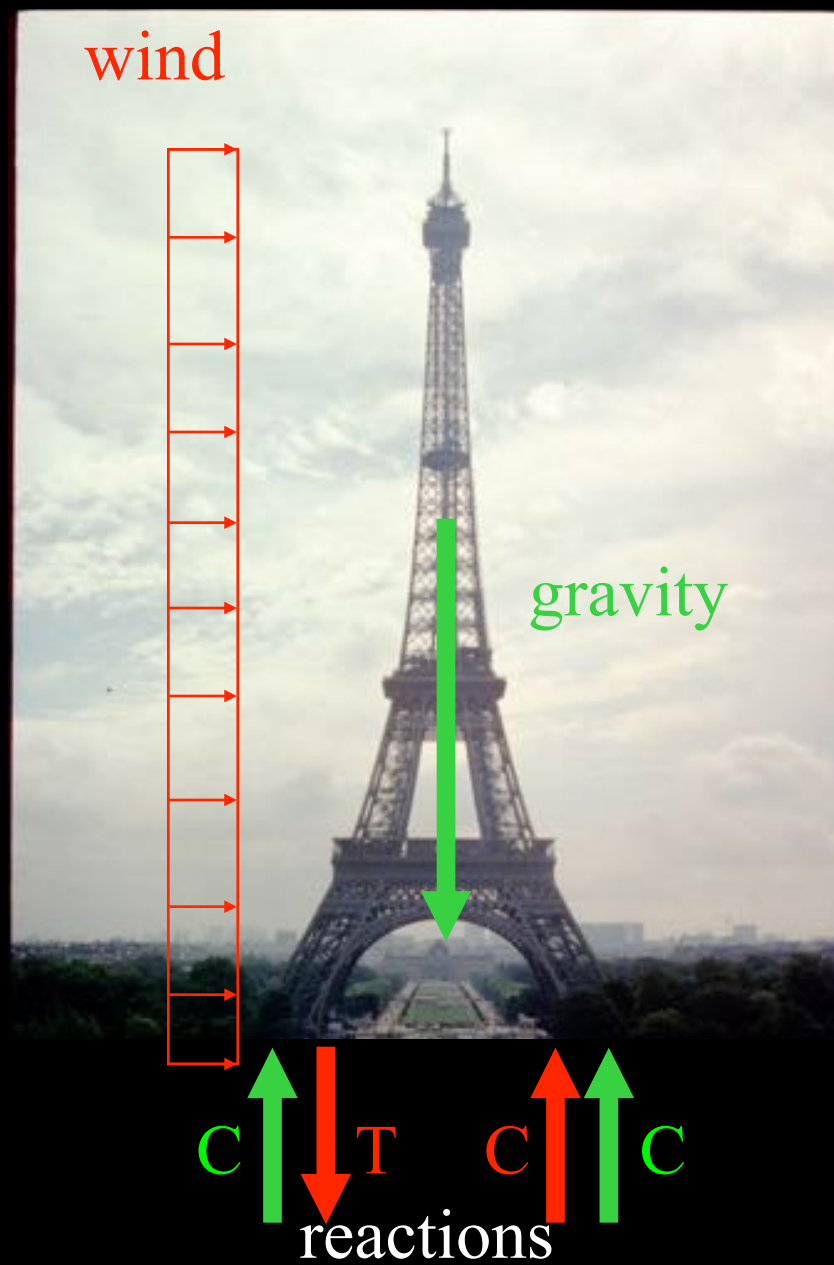
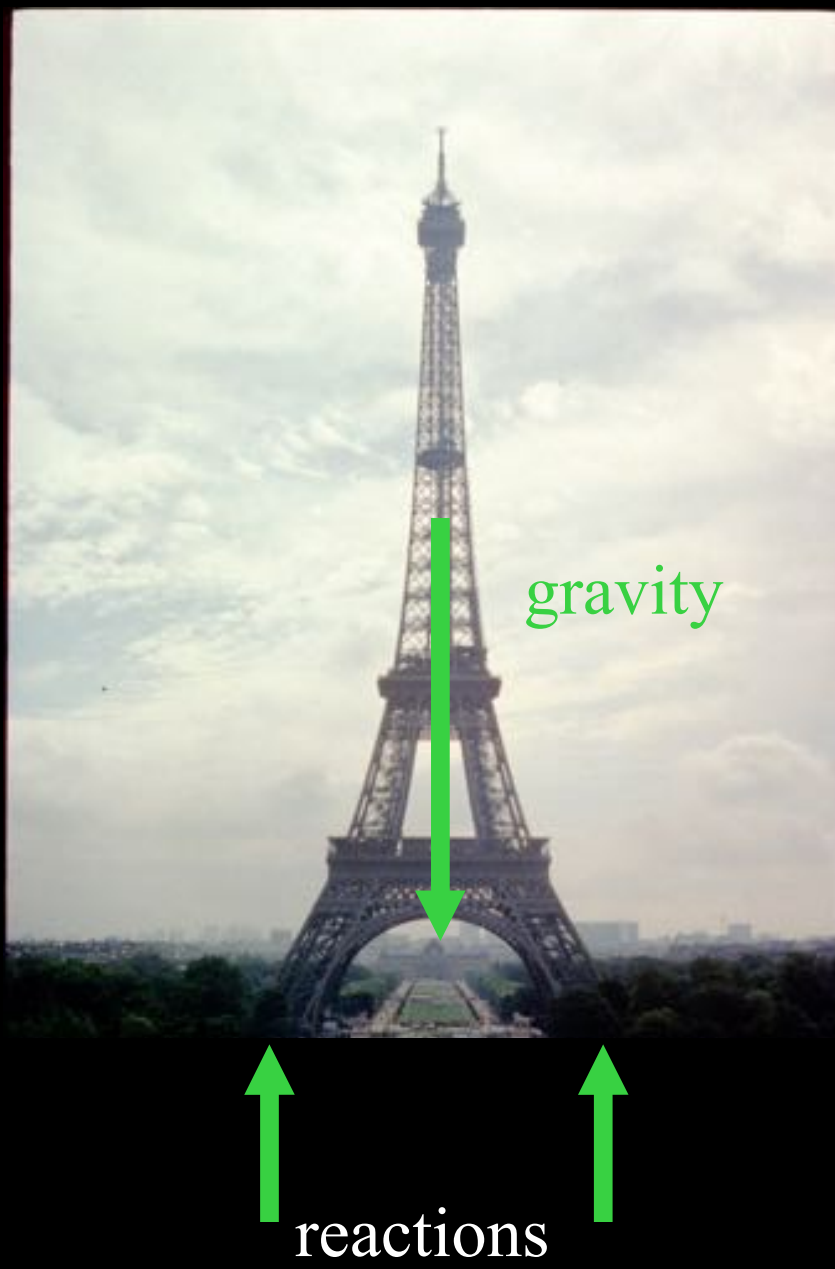


gravity



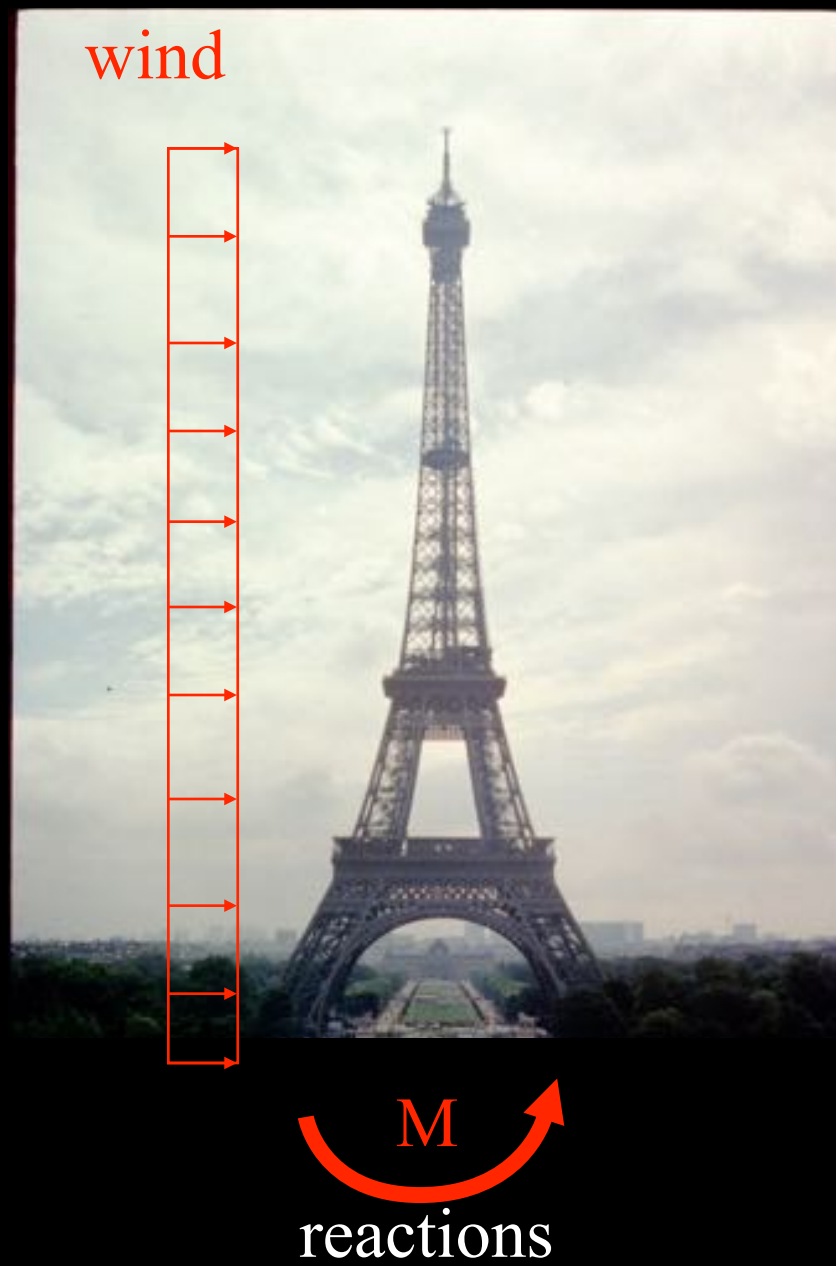
reactions







=



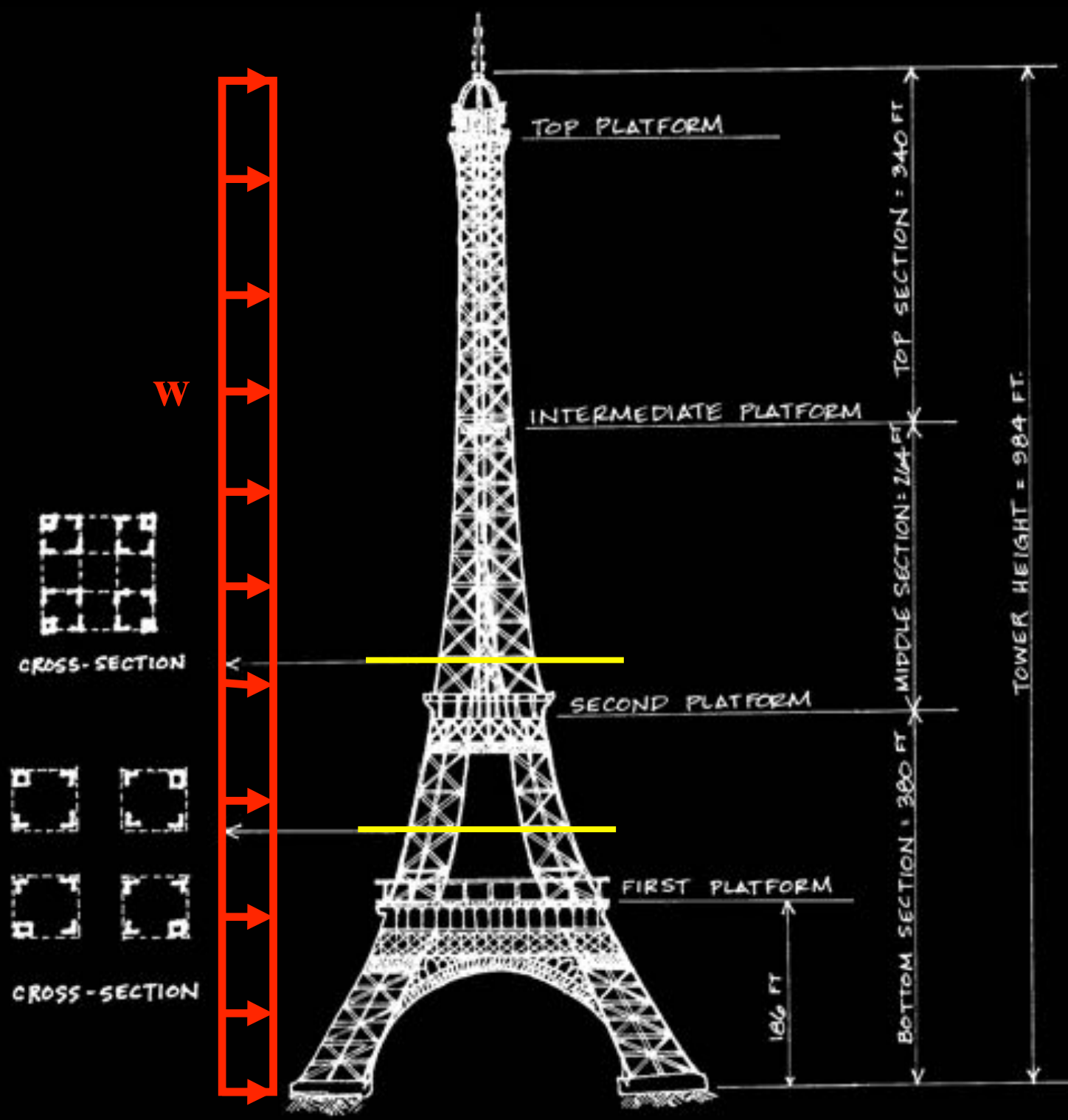
WIND  
FORCE  $P$

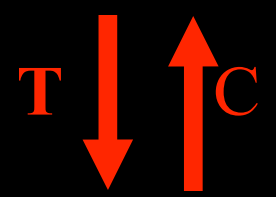
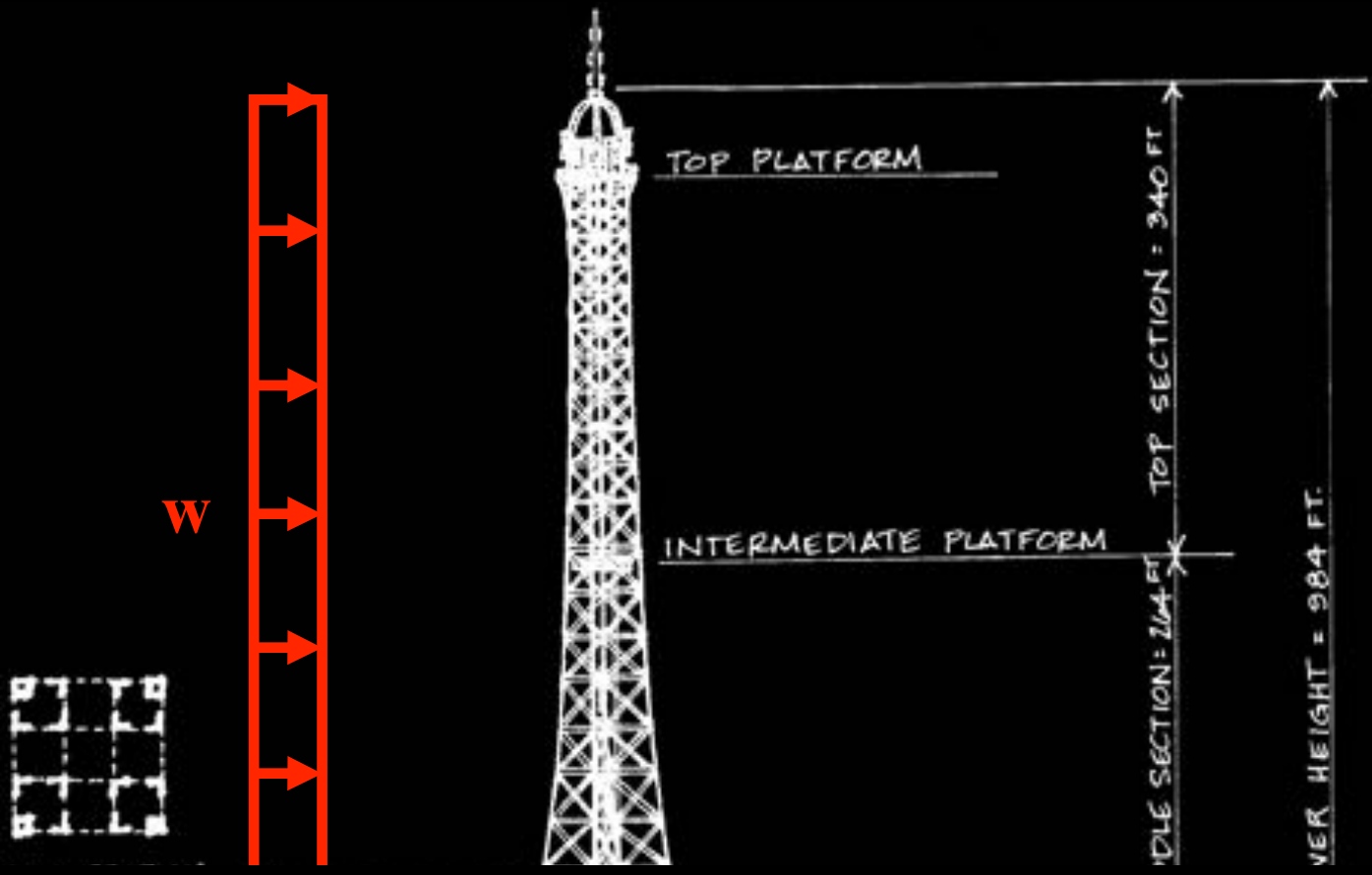


STRETCHING,  
(TENSION)

SHORTENING,  
(COMPRESSION)

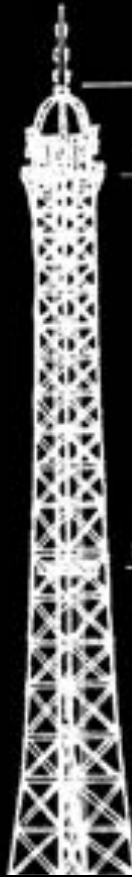








$w$



TOP PLATFORM

INTERMEDIATE PLATFORM

TOP SECTION = 340 FT

BASE SECTION = 244 FT

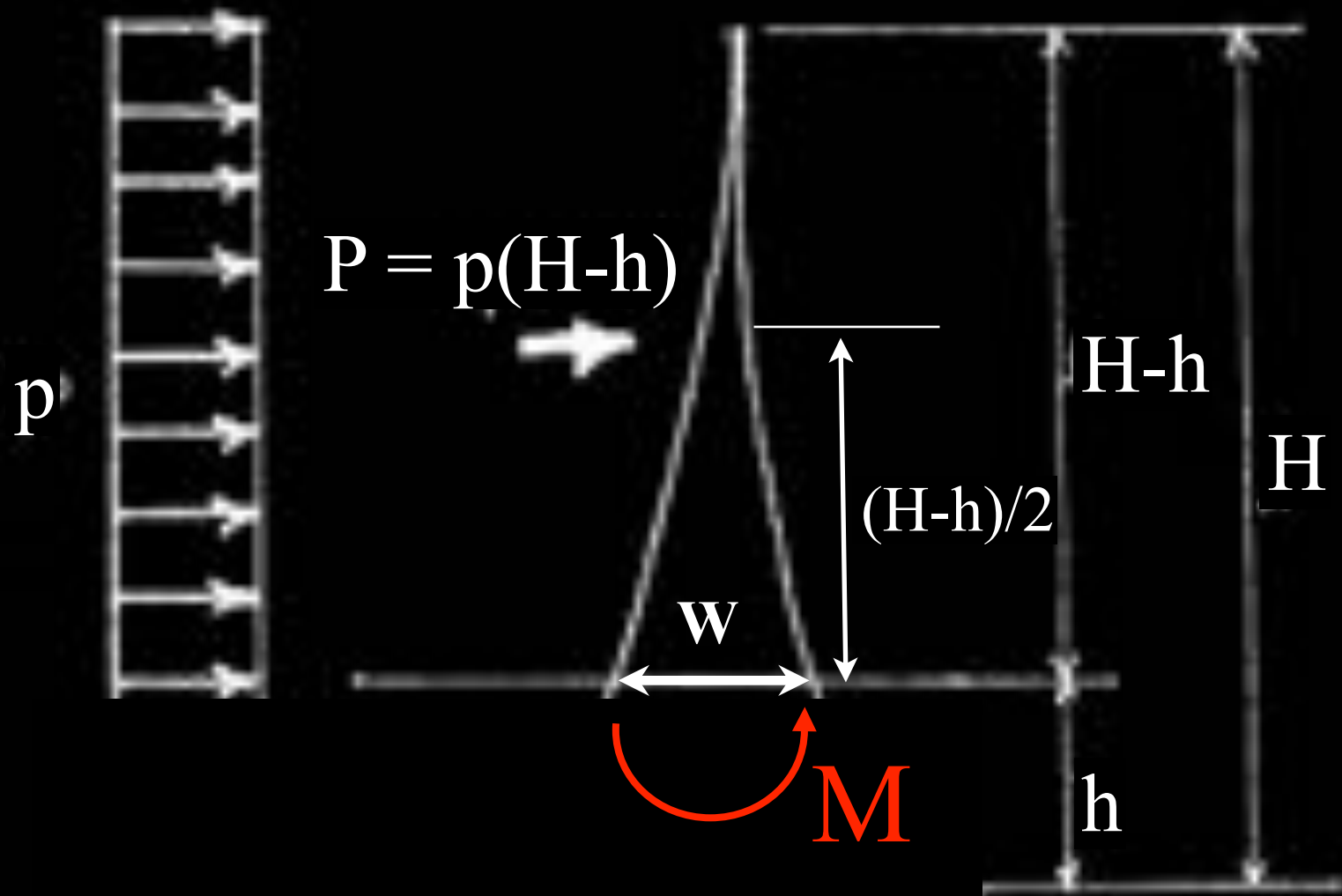
VER HEIGHT = 584 FT



# Civil Engineering Units

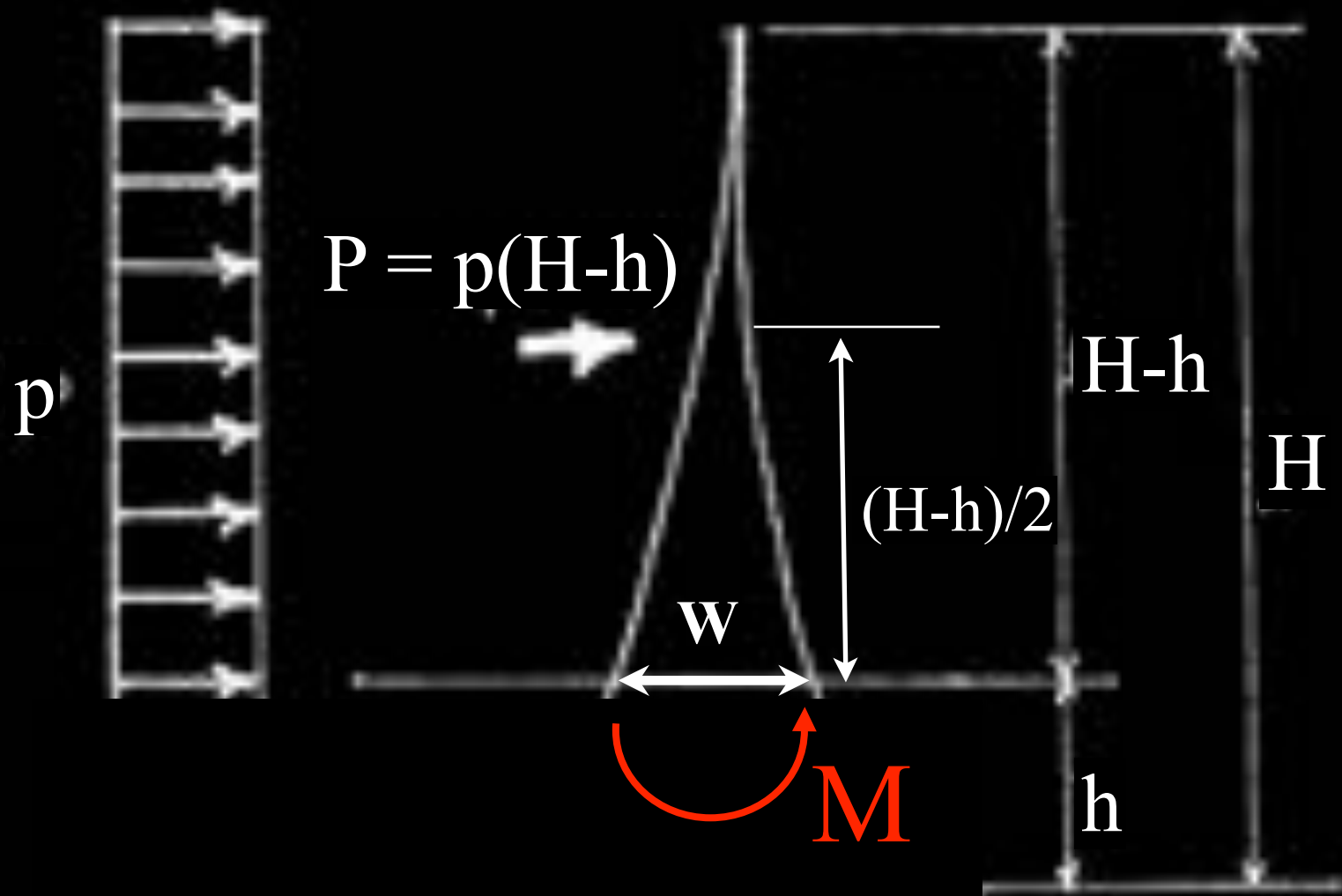
- Lots of imperial units..
- The kip? kip = kilopound = 1000 lb
- The psf? a pound per square foot
  - say you weigh 150 lb and are standing on a part of the floor which is 1ft x 1ft, you are = 150psf
  - other way – say a constant wind of 40 psf is blowing on a building which is 100ft x 100ft across – the force is  $40\text{psf} \times 100\text{ft} \times 100\text{ft} = 40,000 \text{ lb}$
  - $40,000 \text{ lb} = 40 \text{ kips}$
- Also... psi and ksi, pound/sq. in, and kip/sq. in
  - Materials may be described as having limit stresses in psi or ksi, e.g., typical yield stress of steel = 50 ksi

Equilibrium



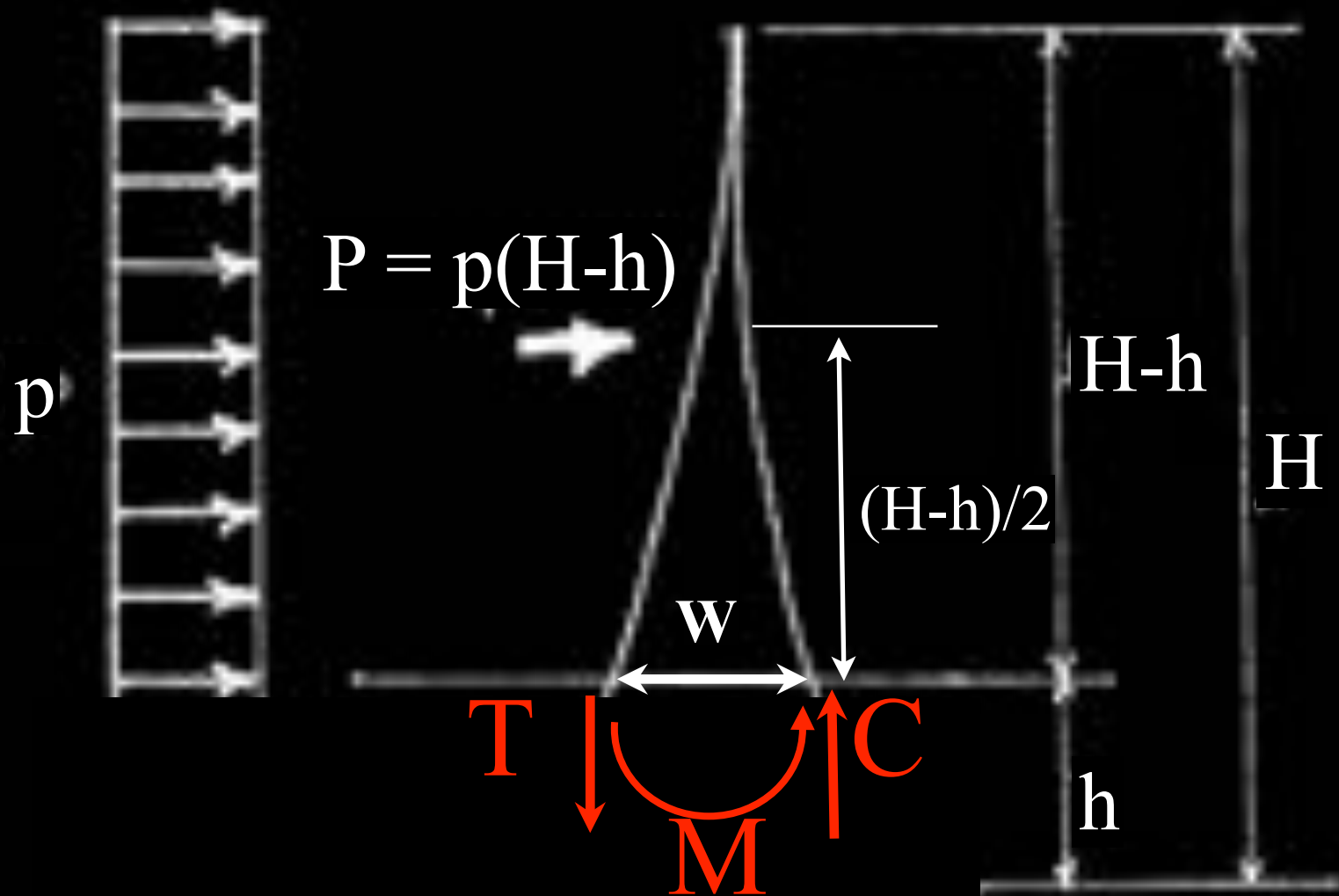
$$\Sigma M_{\text{section}} = 0 \rightarrow M - p(H-h)(H-h)/2 = 0$$





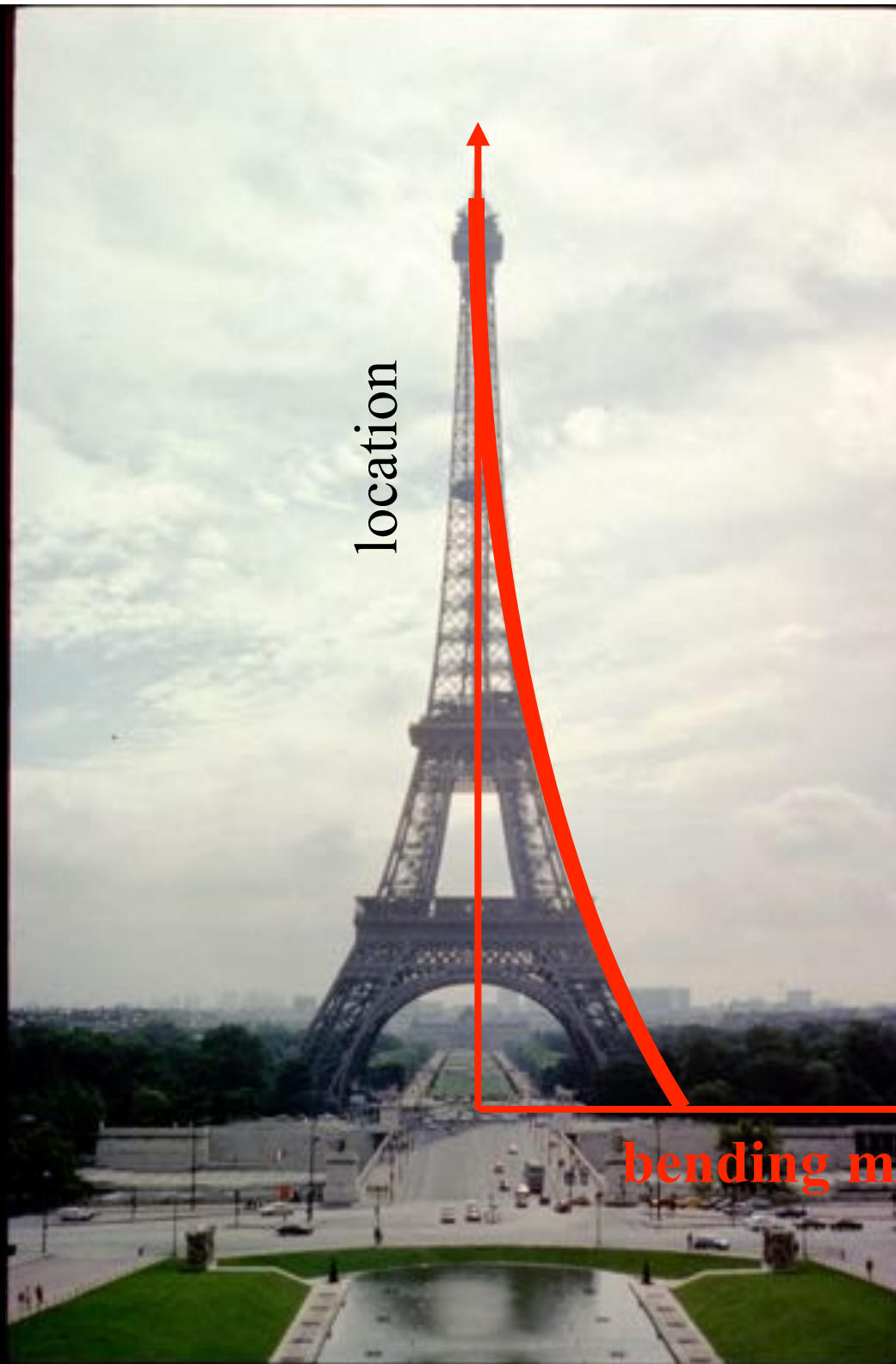
$$\Sigma M_{\text{section}} = 0 \rightarrow M - p(H-h)(H-h)/2 = 0$$

$$M = [p(H-h)][(H-h)/2] = P(H-h)/2$$



$$M = [p(H-h)] \left[ \frac{(H-h)}{2} \right] = P(H-h)/2$$

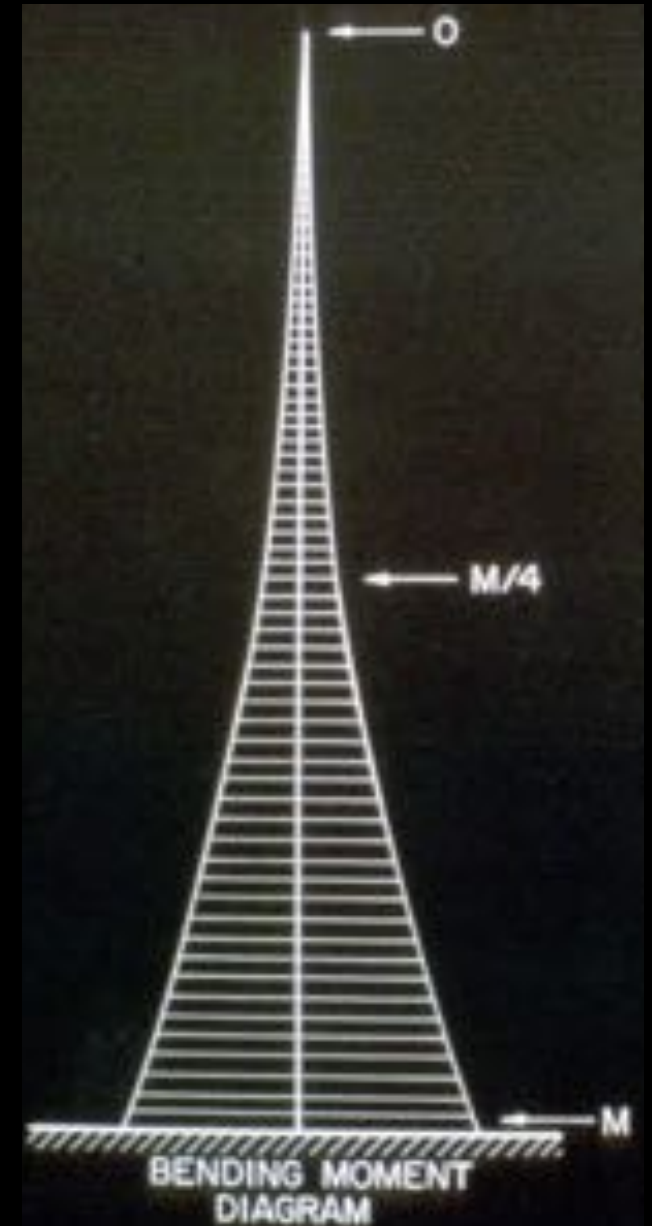
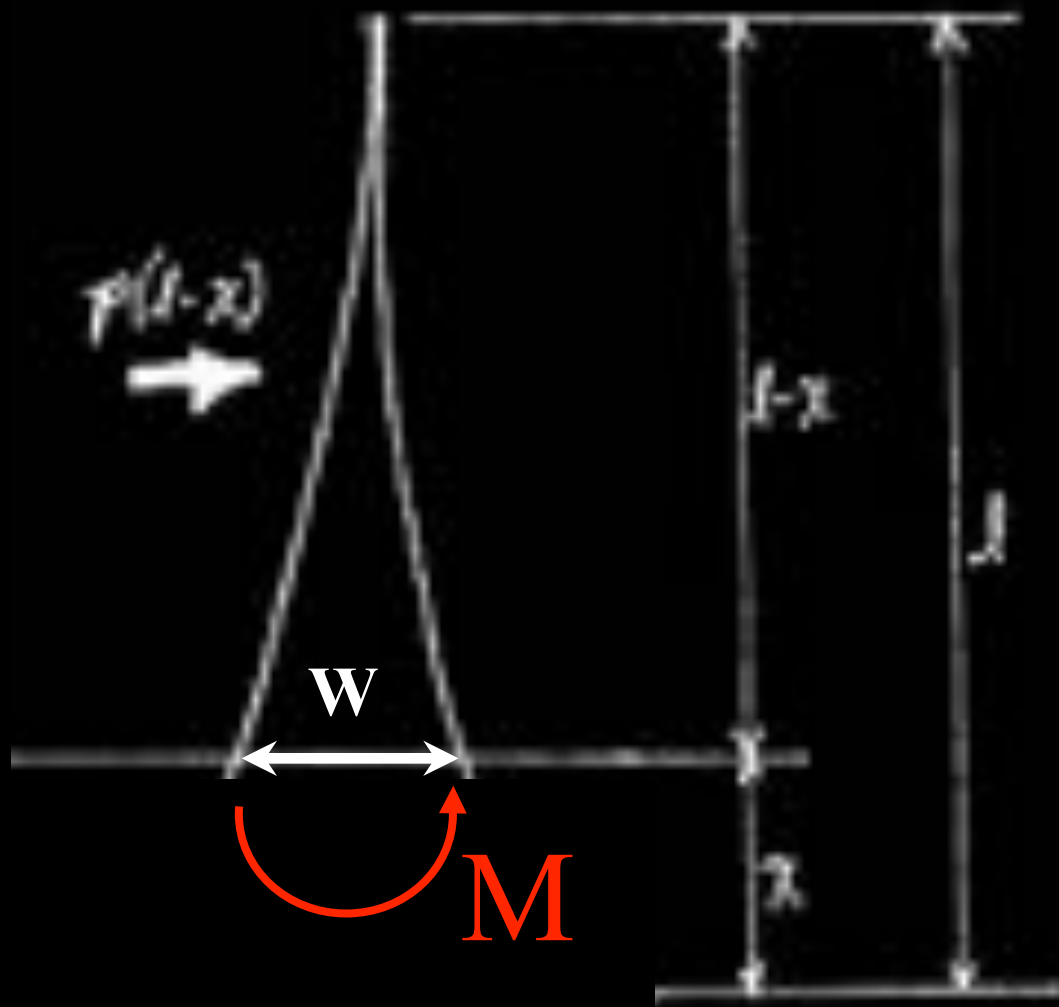
$$C = -T = M/w$$



location

bending moment





$$M = [p(H-h)] \left[ \frac{(H-h)}{2} \right] = \frac{p(H-h)^2}{2}$$

# Load path

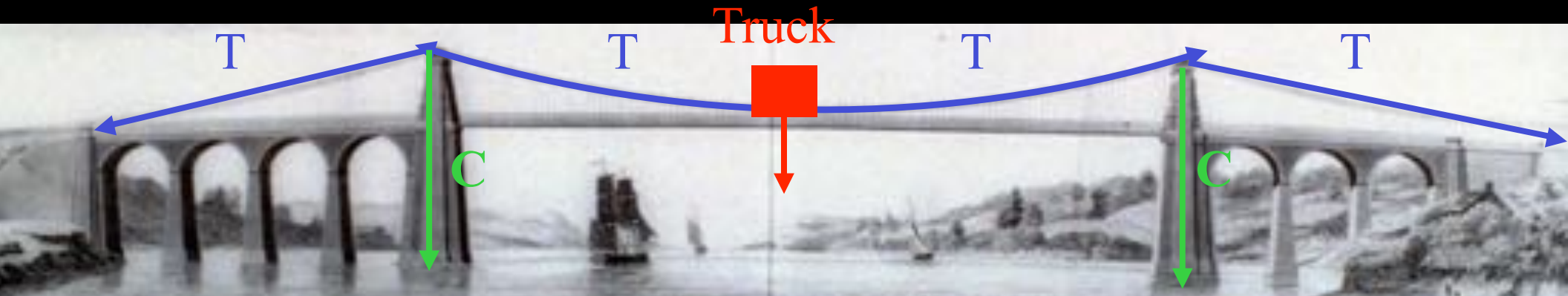
or, how the load travels to the ground

All forces or loads must eventually get to the ground.  
Can we trace the path of tension or compression?



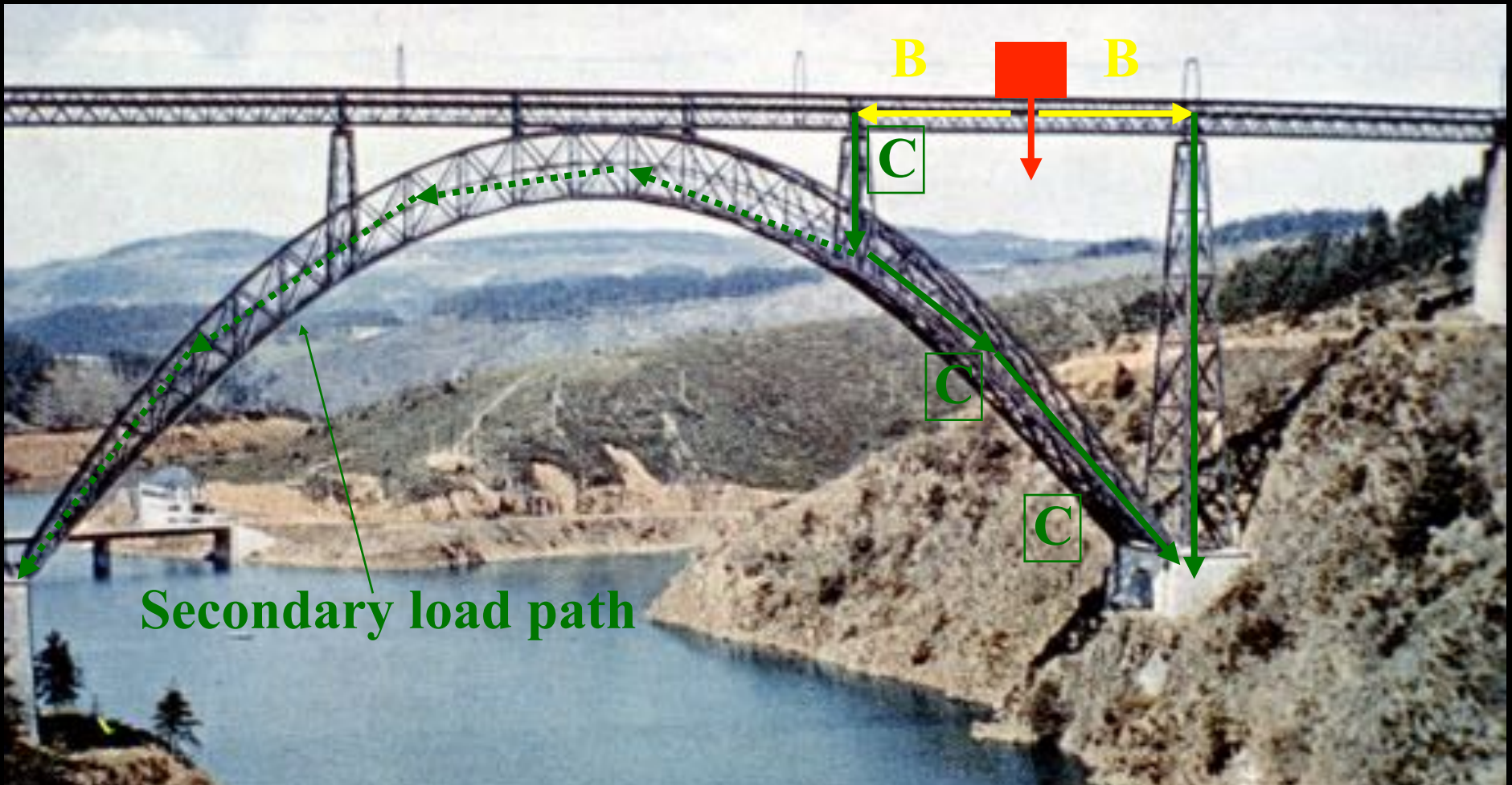


All forces or loads must eventually get to the ground.  
Can we trace the path of tension or compression?

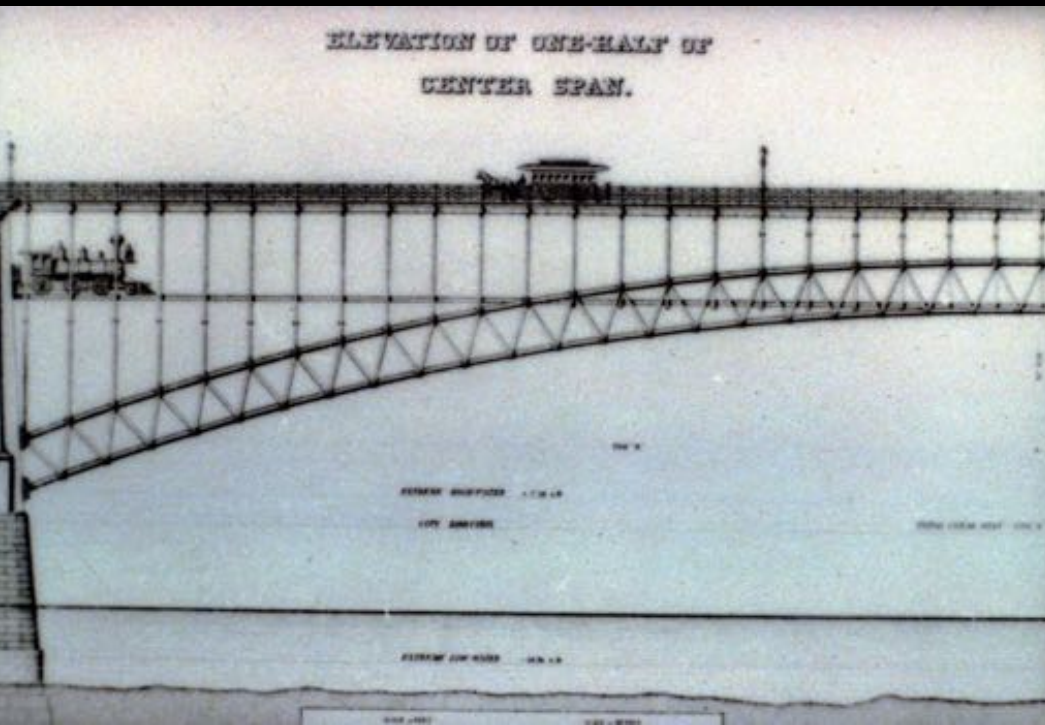


All forces or loads must eventually get to the ground.  
Can we trace the path of tension or compression?

locomotive



Secondary load path



Pick the person on the railing, the carriage, or the locomotive - describe the load path for the force you have selected...